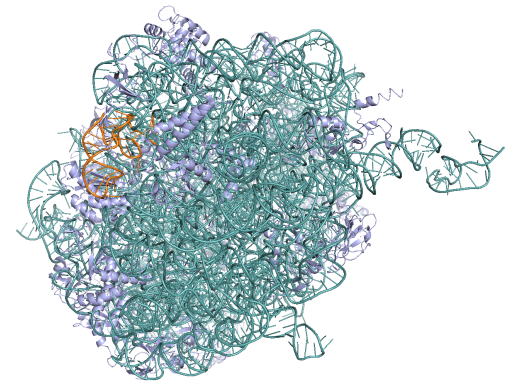


GEOMETRIC PROPERTIES OF RIBOSOMAL STRUCTURES

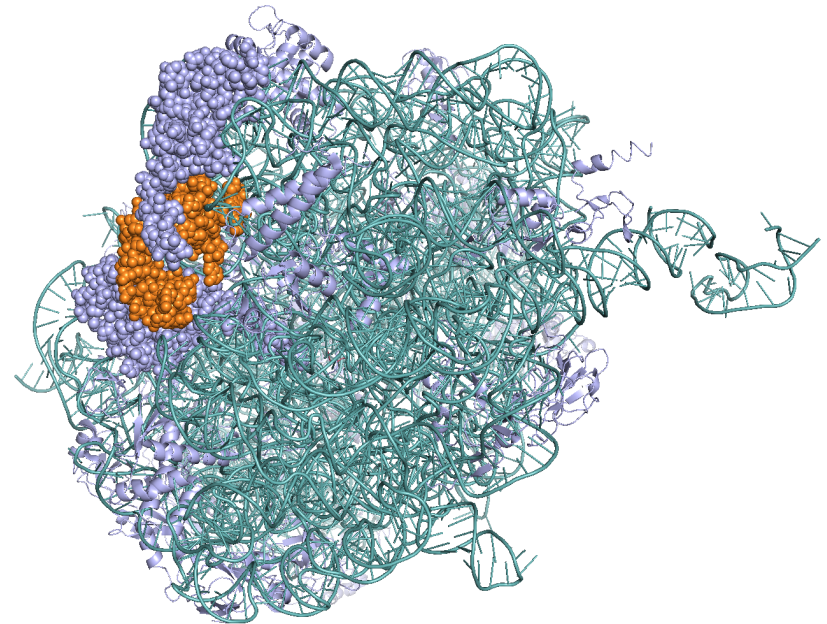
Caitlin Davis, 2019 DIMACS REU



E. Coli ribosome

Ribosomes

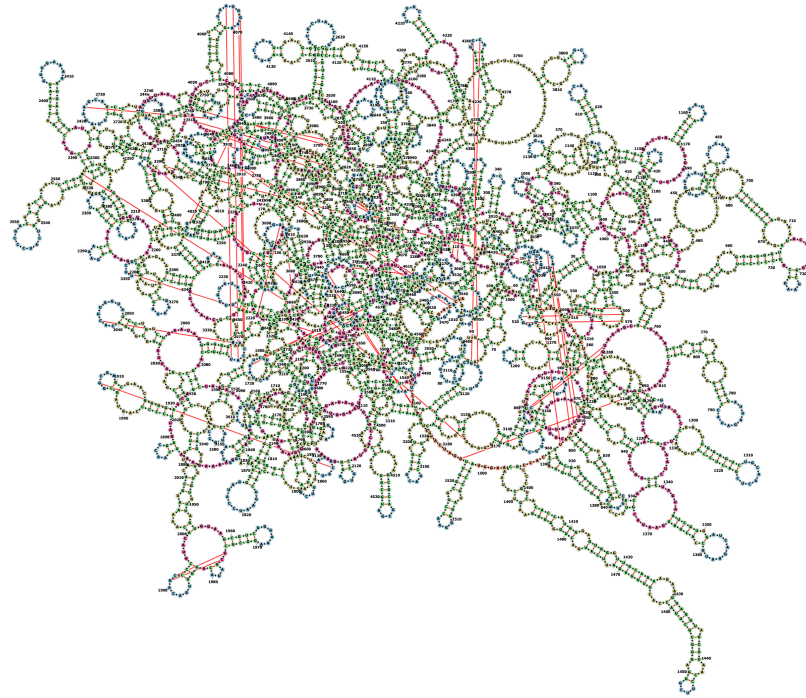
- Location of protein synthesis
- Relatively similar across all species
- Composed of RNA and proteins



E. Coli ribosome

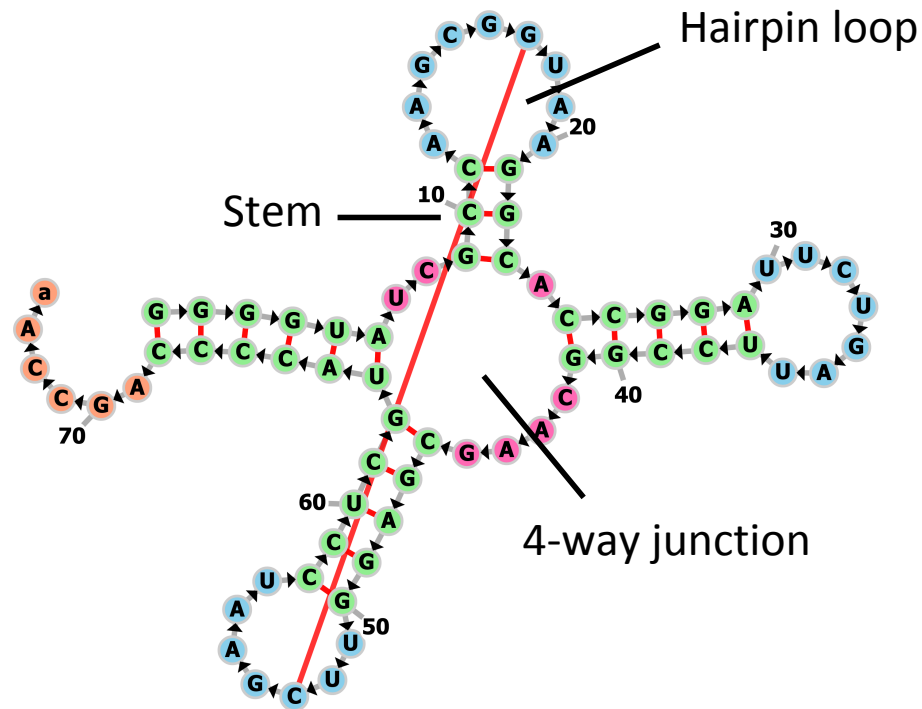
RNA secondary structure

- Typically single-stranded, but bases have some tendency to pair



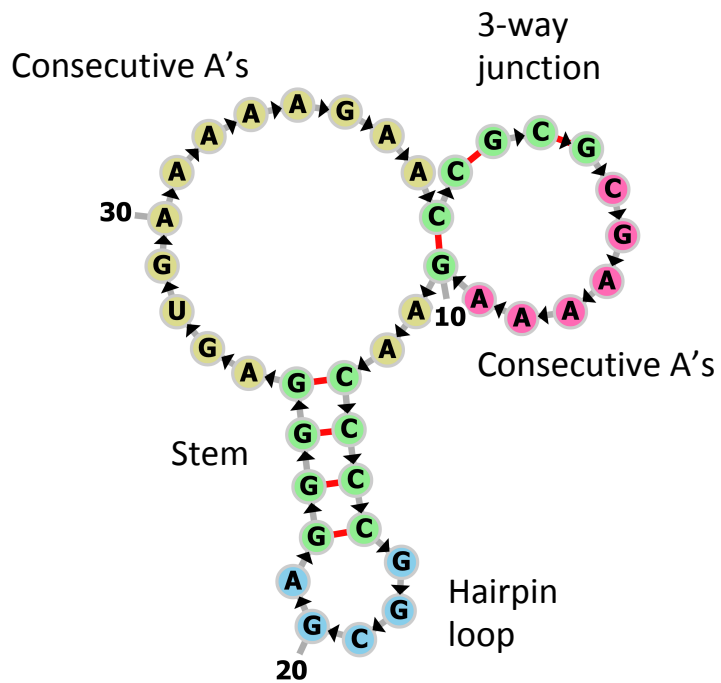
RNA secondary structure

- Often made up of simple, commonly occurring motifs



E. coli transfer RNA molecule

Motif from E. Coli ribosome



2D representation



3D representation

Questions

- In which ribosomes does this motif appear?
- How does the motif differ among ribosomes?

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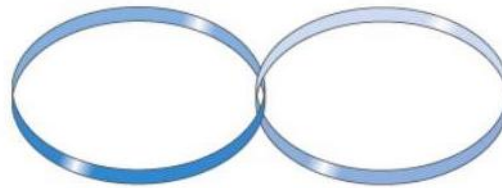
Motif from E. coli
ribosome 3J5L



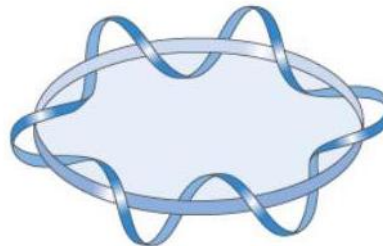
Motif from E. coli
ribosome 3JA1

Topological and geometric properties

- Used to study circular DNA and other nucleic acid structures which are constrained at both ends
- Linking number—describes the number of times two curves wrap around each other



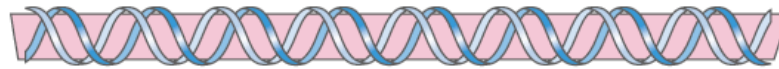
$Lk = 1$
(a)



$Lk = 6$
(b)

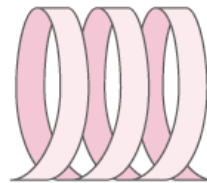
Topological and geometric properties

- Twist—describes the rate of rotation of one curve about another
- Writhing number—describes the non-planarity and non-sphericity of a curve



Straight ribbon (relaxed DNA)

(a)



Large writhe, small change in twist

(b)



Zero writhe, large change in twist

(c)

Writhing number

- The writhing number of a smooth curve can be expressed as a Gauss integral:

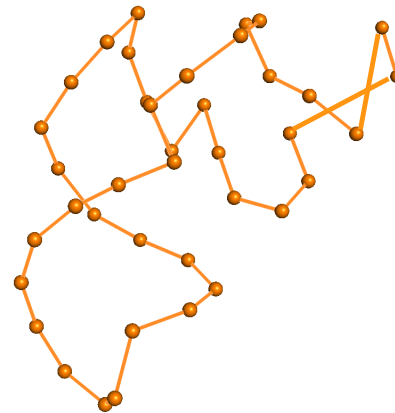
$$\text{Wr}(C) = \frac{1}{4\pi} \oint \oint \frac{t(s') \times t(s) \cdot (\mathbf{r}(s') - \mathbf{r}(s))}{|\mathbf{r}(s') - \mathbf{r}(s)|^3} ds ds'$$

Non-smooth curves

- Geometric information about a molecule consists of the coordinates of all atoms in the molecule
- Instead of fitting a smooth curve to these points, we can study the molecule as a piecewise linear curve



Motif from E. coli
ribosome 3J5L



Discrete curve
representation of motif

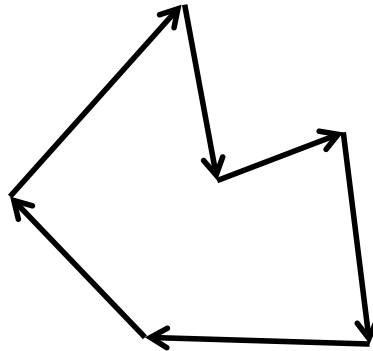
Discrete writhing number

- We compute the discrete writhing number by summing the contribution of each pair of edges in the curve

$$Wr(\{\mathbf{v}_i\}) = \frac{1}{2\pi} \sum_{p,q} w^{pq}$$

- Each pair of edges contributes a quantity involving four dihedral angles:

$$w^{pq} = \xi^{pq}(1, 0) + \xi^{pq}(0, 1) - \xi^{pq}(1, 1) - \xi^{pq}(0, 0)$$



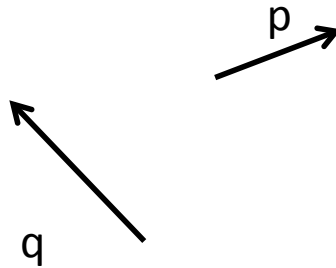
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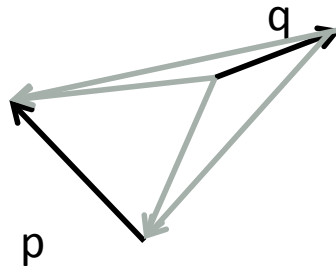
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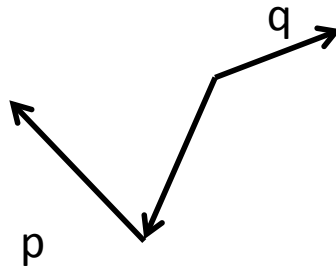
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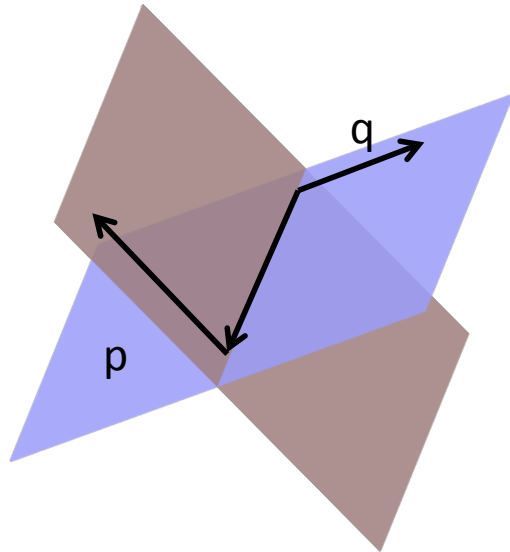
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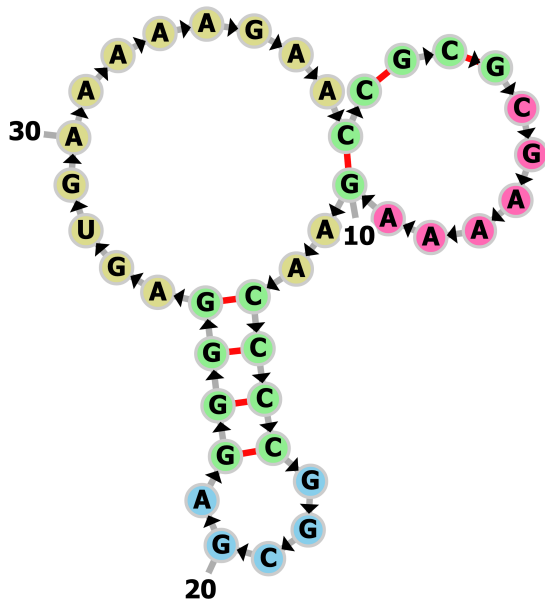
$$Wr(\{\mathbf{v}_i\}) = \frac{1}{2\pi} \sum_{p,q} w^{pq}$$

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Motif from E. Coli ribosome

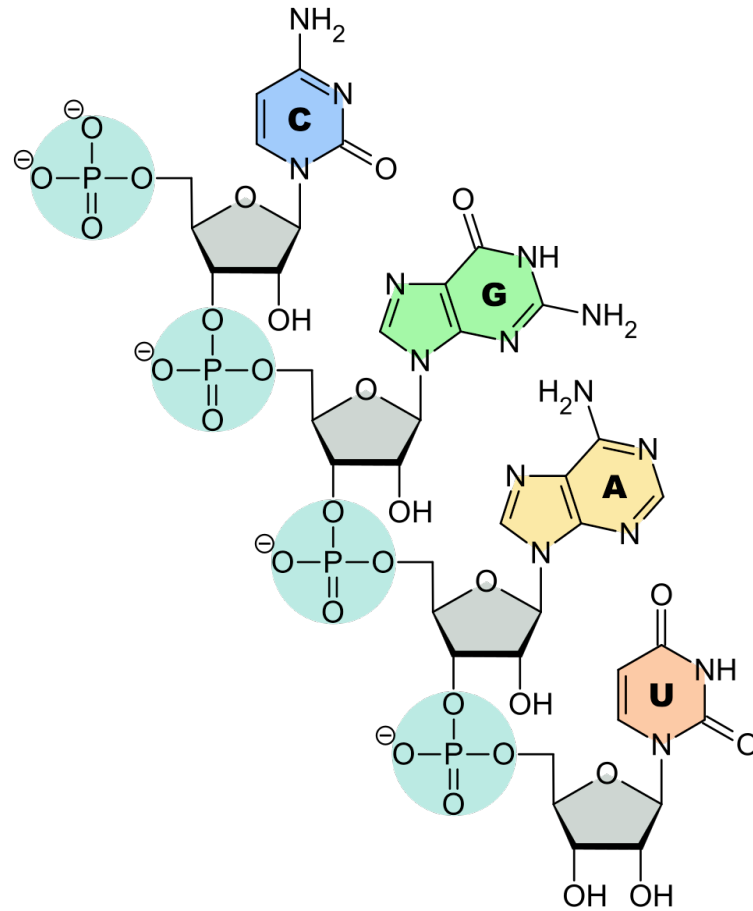


2D representation



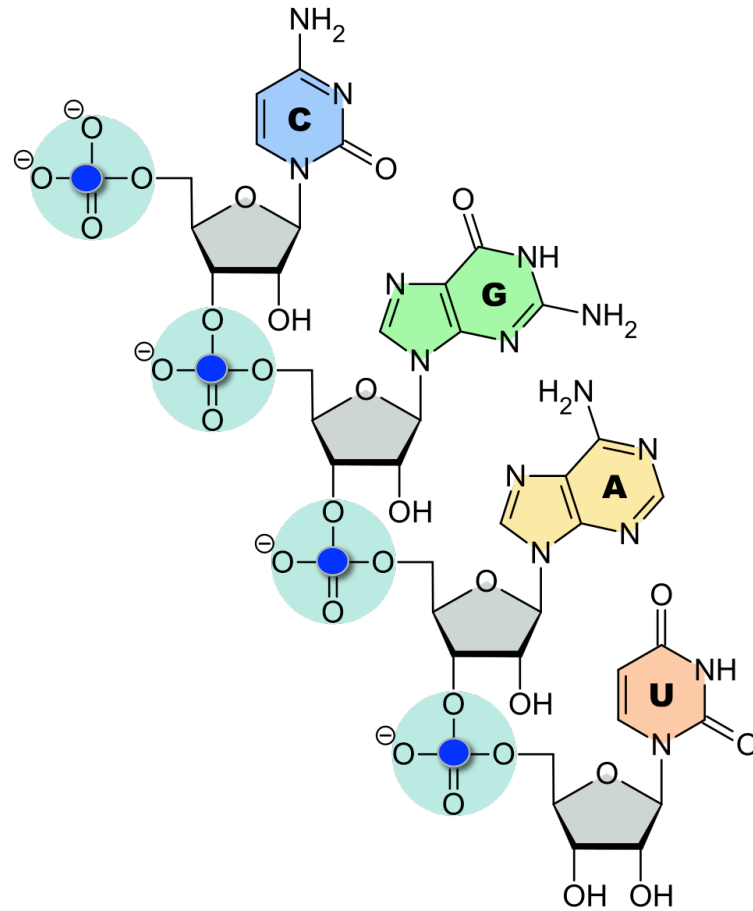
3D representation

RNA structure



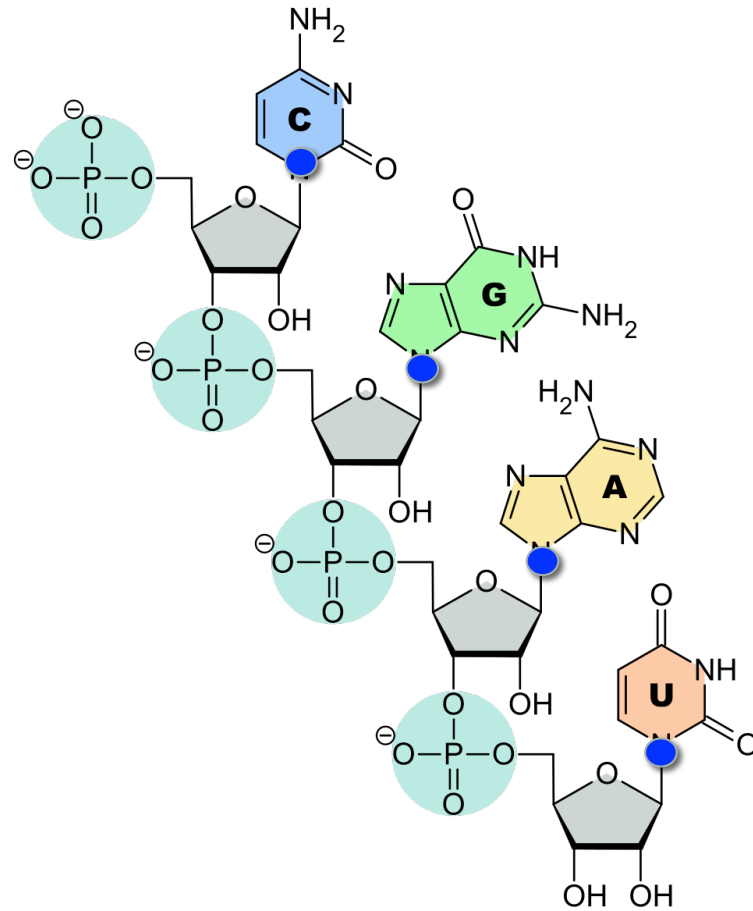
<https://commons.wikimedia.org/wiki/File:RNA-Nucleobases.svg>

RNA structure



<https://commons.wikimedia.org/wiki/File:RNA-Nucleobases.svg>

RNA structure

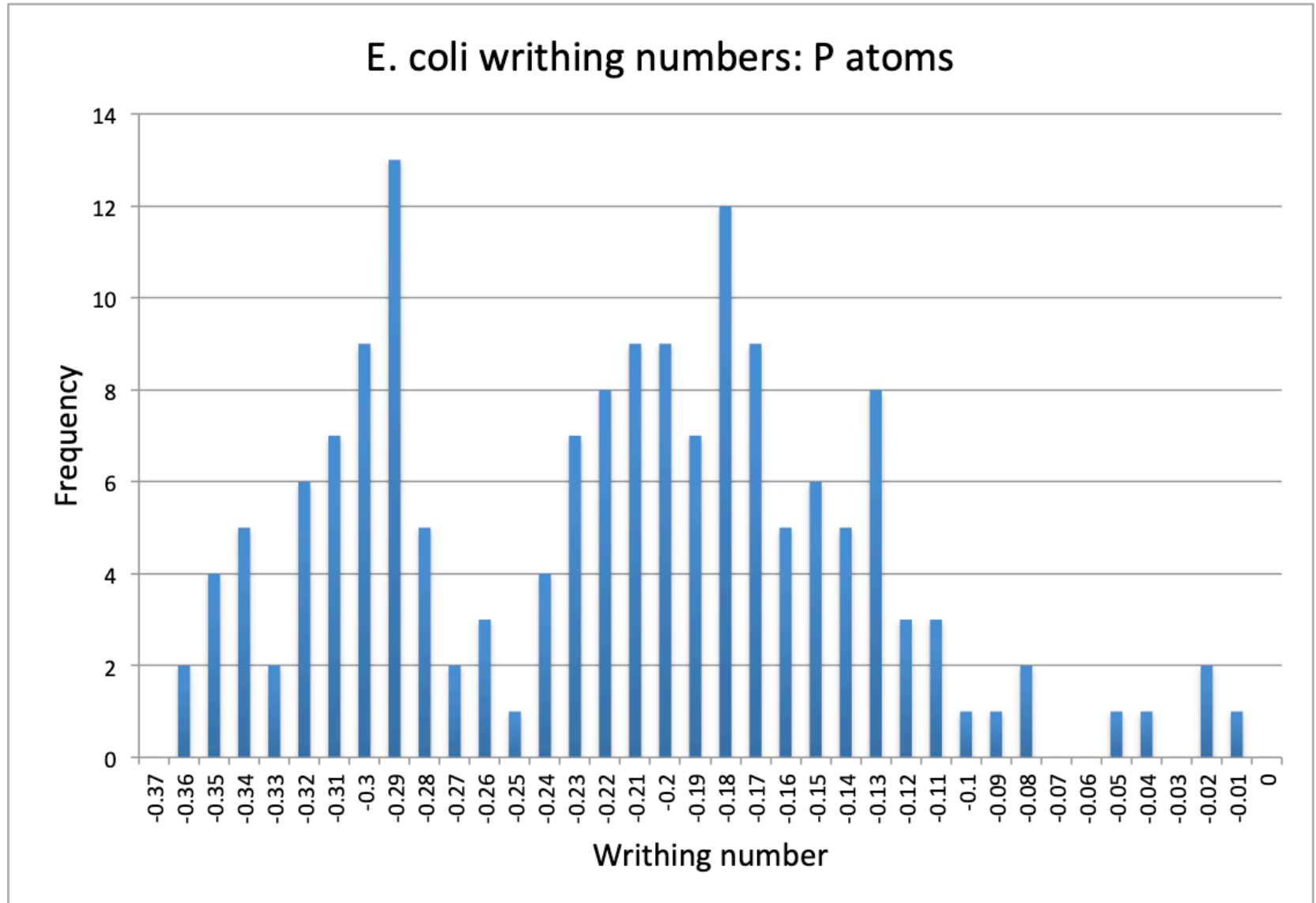


<https://commons.wikimedia.org/wiki/File:RNA-Nucleobases.svg>

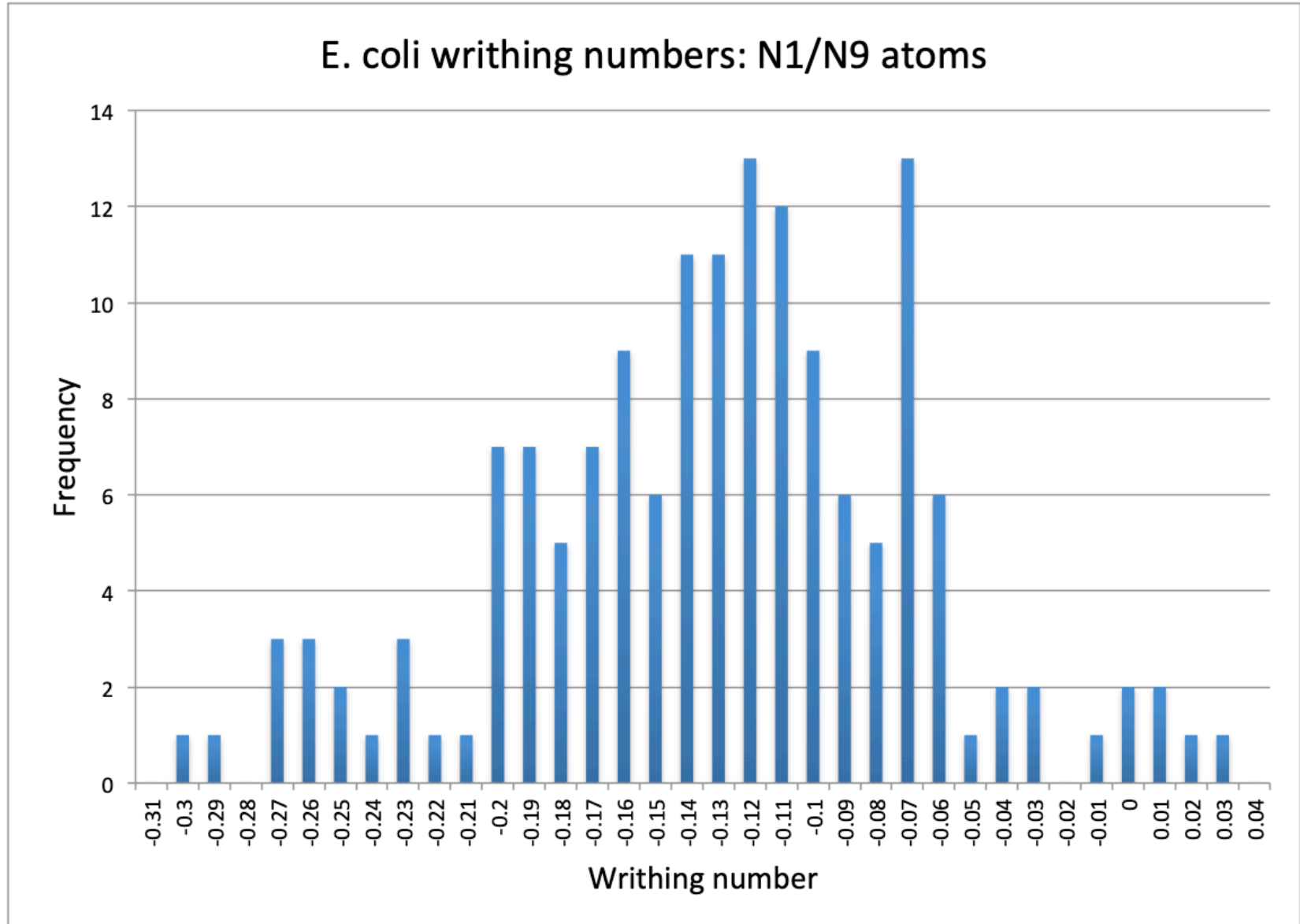
Questions

- How does the choice of vertices affect the writhing number of the motif?
- How does the writhing number of the motif vary across species?
- How does the writhing number of the motif vary across ribosomes of the same species?

Initial observations: E. coli



Initial observations: E. coli



Next steps

- Study characteristics of different *E. coli* ribosomes in order to understand variations in writhing numbers
- Study writhing numbers computed for structures from other species
- Compare results from *E. coli* to those from other species

Acknowledgements

- Thank you to Professor Wilma Olson, and to the Olson group.
- Thank you to the DIMACS REU, and to the NSF, which has provided support through grant CCF-1852215.

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