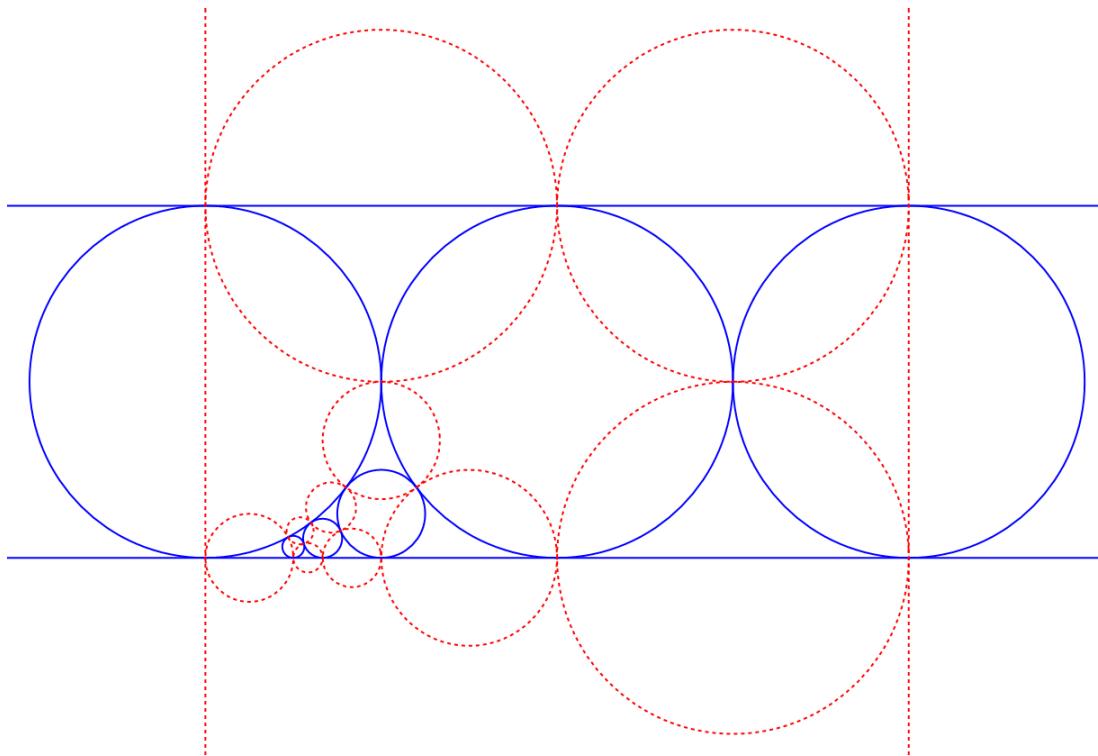


Appendix

For each polyhedron, we have included an adjacency dictionary for the respective edge-graph, a figure showing the cluster and co-cluster, the inversive coordinate vector, the Gram matrix, and the bend matrices. We label each polyhedron by the number of vertices and faces. For example, 8v12f_0 has 8 vertices and 12 faces, and we use “_0” to distinguish from other polyhedra with the same number of vertices and faces.

8v12f_0

```
8v12f_0 = Graph({0:[1, 2, 3, 4, 5, 6, 7], 1:[0, 7, 6, 2], 2:[0, 1, 6, 5, 4, 3], 3:[0, 2, 4], 4:[0, 3, 2, 5],  
5:[0, 4, 2, 6], 6:[0, 5, 2, 1, 7], 7:[0, 6, 1]})
```

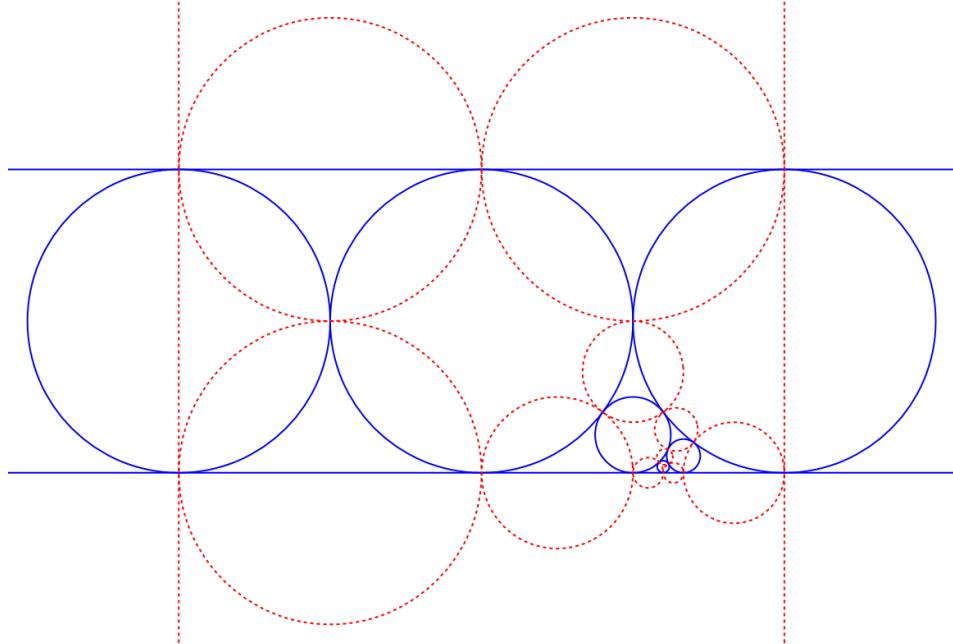


$$V = \begin{pmatrix} 0 & 0 & 0 & -1 \\ 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 4 & 1 & 0 \\ 4 & 16 & 8 & 1 \\ 4 & 13 & 7 & 2 \\ 4 & 12 & 7 & 0 \\ 4 & 9 & 6 & 1 \\ 4 & 7 & 5 & 2 \\ 4 & 6 & 5 & 0 \\ 4 & 4 & 4 & 1 \\ 4 & 3 & 3 & 2 \\ 4 & 2 & 3 & 0 \\ 4 & 1 & 2 & 1 \\ 4 & 1 & 1 & 2 \\ 8 & 1 & 3 & 0 \\ 12 & 1 & 3 & 2 \\ 16 & 1 & 4 & 1 \\ 4 & 0 & 0 & 1 \\ 8 & 0 & 1 & 0 \end{pmatrix}$$

$$G = \begin{pmatrix} -1 & 0 & 1 & 0 & 1 & 2 & 0 & 1 & 2 & 0 & 1 & 2 & 0 & 1 & 2 & 0 & 2 & 1 & 1 & 1 & 0 \\ 0 & -1 & 0 & 1 & 8 & 7 & 7 & 6 & 5 & 5 & 4 & 3 & 3 & 2 & 1 & 3 & 3 & 4 & 0 & 1 \\ 1 & 0 & -1 & 0 & 1 & 0 & 2 & 1 & 0 & 2 & 1 & 0 & 2 & 1 & 0 & 4 & 4 & 7 & 1 & 4 \\ 0 & 1 & 0 & -1 & 0 & 1 & 1 & 2 & 3 & 3 & 4 & 5 & 5 & 6 & 7 & 13 & 21 & 28 & 8 & 15 \\ 1 & 8 & 1 & 0 & -1 & 0 & 0 & 1 & 4 & 4 & 7 & 12 & 12 & 17 & 24 & 42 & 72 & 97 & 31 & 56 \\ 2 & 7 & 0 & 1 & 0 & -1 & 1 & 0 & 1 & 3 & 4 & 7 & 9 & 12 & 17 & 33 & 55 & 76 & 24 & 45 \\ 0 & 7 & 2 & 1 & 0 & 1 & -1 & 0 & 3 & 1 & 4 & 9 & 7 & 12 & 19 & 29 & 53 & 70 & 24 & 41 \\ 1 & 6 & 1 & 2 & 1 & 0 & 0 & -1 & 0 & 0 & 1 & 4 & 4 & 7 & 12 & 20 & 36 & 49 & 17 & 30 \\ 2 & 5 & 0 & 3 & 4 & 1 & 3 & 0 & -1 & 1 & 0 & 1 & 3 & 4 & 7 & 15 & 25 & 36 & 12 & 23 \\ 0 & 5 & 2 & 3 & 4 & 3 & 1 & 0 & 1 & -1 & 0 & 3 & 1 & 4 & 9 & 11 & 23 & 30 & 12 & 19 \\ 1 & 4 & 1 & 4 & 7 & 4 & 4 & 1 & 0 & 0 & -1 & 0 & 0 & 1 & 4 & 6 & 12 & 17 & 7 & 12 \\ 2 & 3 & 0 & 5 & 12 & 7 & 9 & 4 & 1 & 3 & 0 & -1 & 1 & 0 & 1 & 5 & 7 & 12 & 4 & 9 \\ 0 & 3 & 2 & 5 & 12 & 9 & 7 & 4 & 3 & 1 & 0 & 1 & -1 & 0 & 3 & 1 & 5 & 6 & 4 & 5 \\ 1 & 2 & 1 & 6 & 17 & 12 & 12 & 7 & 4 & 4 & 1 & 0 & 0 & -1 & 0 & 0 & 0 & 1 & 1 & 2 \\ 2 & 1 & 0 & 7 & 24 & 17 & 19 & 12 & 7 & 9 & 4 & 1 & 3 & 0 & -1 & 3 & 1 & 4 & 0 & 3 \\ 0 & 3 & 4 & 13 & 42 & 33 & 29 & 20 & 15 & 11 & 6 & 5 & 1 & 0 & 3 & -1 & 1 & 0 & 2 & 1 \\ 2 & 3 & 4 & 21 & 72 & 55 & 53 & 36 & 25 & 23 & 12 & 7 & 5 & 0 & 1 & 1 & -1 & 0 & 0 & 1 \\ 1 & 4 & 7 & 28 & 97 & 76 & 70 & 49 & 36 & 30 & 17 & 12 & 6 & 1 & 4 & 0 & 0 & -1 & 1 & 0 \\ 1 & 0 & 1 & 8 & 31 & 24 & 24 & 17 & 12 & 12 & 7 & 4 & 4 & 1 & 0 & 2 & 0 & 1 & -1 & 0 \\ 0 & 1 & 4 & 15 & 56 & 45 & 41 & 30 & 23 & 19 & 12 & 9 & 5 & 2 & 3 & 1 & 1 & 0 & 0 & -1 \end{pmatrix}$$

$$\begin{array}{l}
\left\{ \left(\begin{array}{cccc} 0 & 0 & 0 & 2 \\ 0 & 0 & 0 & 28 \\ 0 & 0 & 0 & 45 \\ 0 & 0 & 0 & 66 \\ 0 & 0 & 0 & 91 \\ 0 & 0 & 0 & 420 \end{array} \right), \text{integral} \right\}, \left\{ \left(\begin{array}{cccc} 0 & 0 & 0 & 12 \\ 0 & 0 & 0 & 88 \\ 0 & 0 & 0 & 35 \\ 0 & 0 & 0 & 6 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 20 \end{array} \right), \text{integral} \right\}, \left\{ \left(\begin{array}{cccc} 0 & 0 & 0 & 2 \\ 0 & 0 & 0 & 100 \\ 0 & 0 & 0 & 51 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{array} \right), \text{integral} \right\}, \left\{ \left(\begin{array}{cccc} 0 & 0 & 0 & 84 \\ 0 & 0 & 0 & 28 \\ 0 & 0 & 0 & 15 \\ 0 & 0 & 0 & 170 \\ 0 & 0 & 0 & 2870 \\ 0 & 0 & 0 & 0 \end{array} \right), \text{integral} \right\}, \left\{ \left(\begin{array}{cccc} -3 & 12 & 4 \\ -24 & 96 & 33 \\ -10 & 38 & 14 \\ -2 & 6 & 3 \\ -5 & 30 & 6 \\ -4 & 20 & 5 \end{array} \right), \text{integral} \right\}, \left\{ \left(\begin{array}{cccc} -36 & 60 & 93 \\ -18 & 30 & 46 \\ -6 & 10 & 15 \\ -3 & 4 & 12 \\ -2 & 3 & 6 \\ 0 & 0 & 1 \end{array} \right), \text{integral} \right\}, \left\{ \left(\begin{array}{cccc} -35 & 108 & 60 \\ -12 & 36 & 21 \\ -6 & 18 & 10 \\ -70 & 218 & 119 \\ -2870 & 3710 & 2030 \\ 0 & 1 & 0 \end{array} \right), \text{integral} \right\}, \left\{ \left(\begin{array}{cccc} 84 & -35 & 108 & 60 \\ 28 & -12 & 36 & 21 \\ 15 & -6 & 18 & 10 \\ 170 & -70 & 218 & 119 \\ 2870 & -1189 & 3710 & 2030 \\ 408 & 1272 & 697 \end{array} \right), \text{integral} \right\} \\
\\
\left\{ \left(\begin{array}{cccc} 0 & 0 & 0 & 2 \\ 0 & 0 & 0 & 120 \\ 0 & 0 & 0 & 15 \\ 0 & 0 & 0 & 6 \\ 0 & 0 & 0 & 93 \\ 0 & 0 & 0 & 46 \\ 0 & 0 & 0 & 276 \end{array} \right), \text{integral} \right\}, \left\{ \left(\begin{array}{cccc} 0 & 0 & 0 & 2 \\ 0 & 0 & 0 & 28 \\ 0 & 0 & 0 & 15 \\ 0 & 0 & 0 & 186 \\ 0 & 0 & 0 & 541 \\ 0 & 0 & 0 & 90 \\ 0 & 0 & 0 & 1080 \end{array} \right), \text{integral} \right\}, \left\{ \left(\begin{array}{cccc} 0 & 0 & 0 & 6 \\ 0 & 0 & 0 & 70 \\ 0 & 0 & 0 & 35 \\ 0 & 0 & 0 & 12 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 2 \end{array} \right), \text{integral} \right\}, \left\{ \left(\begin{array}{cccc} 3 & 6 & -2 \\ 30 & 78 & -21 \\ 14 & 38 & -10 \\ 4 & 12 & -3 \\ 0 & 0 & 0 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \\ 2 & 2 & -1 \end{array} \right), \text{integral} \right\}, \left\{ \left(\begin{array}{cccc} 6 & 3 & -2 & 6 \\ 100 & 60 & -36 & 93 \\ 51 & 30 & -18 & 46 \\ 18 & 10 & -6 & 15 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 2 & -1 \\ 0 & 0 & 0 & 1 \end{array} \right), \text{integral} \right\} \\
\\
\left\{ \left(\begin{array}{cccc} 0 & 0 & 0 & 40 \\ 0 & 0 & 0 & 104 \\ 0 & 0 & 0 & 15 \\ 0 & 0 & 0 & 6 \\ 0 & 0 & 0 & 77 \\ 0 & 0 & 0 & 570 \end{array} \right), \text{integral} \right\}, \left\{ \left(\begin{array}{cccc} 0 & 0 & 0 & 2 \\ 0 & 0 & 0 & 136 \\ 0 & 0 & 0 & 51 \\ 0 & 0 & 0 & 6 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 36 \end{array} \right), \text{integral} \right\}, \left\{ \left(\begin{array}{cccc} -1 & 2 & 2 & 2 \\ -48 & 120 & 81 \\ -18 & 46 & 30 \\ -2 & 6 & 3 \\ 0 & 0 & 0 & 0 \\ -12 & 28 & 21 \end{array} \right), \text{integral} \right\}, \left\{ \left(\begin{array}{cccc} -2 & 3 & 6 & 6 \\ -28 & 44 & 92 & 77 \\ -15 & 24 & 48 & 40 \\ -6 & 10 & 18 & 15 \\ -1 & 2 & 2 & 2 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{array} \right), \text{integral} \right\}, \left\{ \left(\begin{array}{cccc} 2 & -1 & 2 & 2 \\ 36 & -20 & 60 & 45 \\ 21 & -12 & 36 & 28 \\ 10 & -6 & 18 & 15 \\ 3 & -2 & 6 & 6 \\ 4 & -3 & 12 & 12 \\ 1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{array} \right), \text{integral} \right\} \\
\end{array}$$

8v12f_1



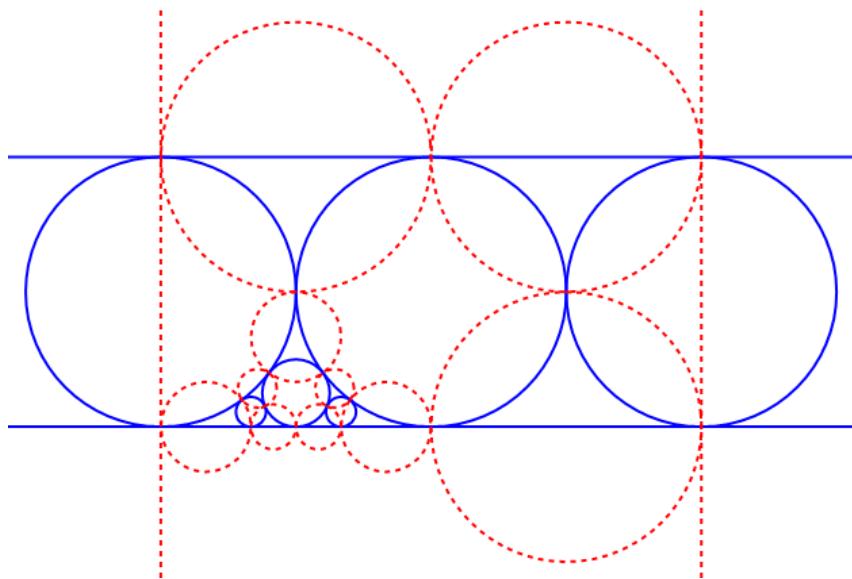
8v12f_1=Graph({ 0:[1, 2, 3, 4, 5, 6, 7], 1:[0, 7, 3, 2], 2:[0, 1, 3], 3:[0, 2, 1, 7, 4], 4:[0, 3, 7, 6, 5], 5:[0, 4, 6], 6:[0, 5, 4, 7], 7:[0, 6, 4, 3, 1] })

$$V = \begin{pmatrix} 0 & 0 & 0 & -1 \\ 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 1 & 1 & 0 \\ 4 & 1 & 2 & 1 \\ 4 & 1 & 1 & 2 \\ 12 & 2 & 5 & 0 \\ 12 & 1 & 3 & 2 \\ 36 & 4 & 12 & 1 \\ 28 & 3 & 9 & 2 \\ 16 & 1 & 4 & 1 \\ 96 & 10 & 31 & 0 \\ 256 & 25 & 80 & 1 \\ 196 & 19 & 61 & 2 \\ 100 & 9 & 30 & 1 \\ 76 & 7 & 23 & 2 \\ 40 & 3 & 11 & 0 \\ 160 & 15 & 49 & 0 \\ 4 & 0 & 0 & 1 \\ 8 & 0 & 1 & 0 \end{pmatrix}$$

$$G = \begin{pmatrix} -1 & 0 & 1 & 0 & 1 & 2 & 0 & 2 & 1 & 2 & 1 & 0 & 1 & 2 & 1 & 2 & 0 & 0 & 1 & 0 & 0 \\ 0 & -1 & 0 & 1 & 2 & 1 & 5 & 3 & 12 & 9 & 4 & 31 & 80 & 61 & 30 & 23 & 11 & 49 & 0 & 1 \\ 1 & 0 & -1 & 0 & 1 & 0 & 6 & 4 & 17 & 12 & 7 & 48 & 127 & 96 & 49 & 36 & 20 & 80 & 1 & 4 \\ 0 & 1 & 0 & -1 & 0 & 1 & 1 & 3 & 6 & 5 & 4 & 17 & 48 & 37 & 20 & 15 & 9 & 31 & 2 & 3 \\ 1 & 2 & 1 & 0 & -1 & 0 & 0 & 0 & 1 & 0 & 1 & 6 & 17 & 12 & 7 & 4 & 4 & 12 & 1 & 2 \\ 2 & 1 & 0 & 1 & 0 & -1 & 5 & 1 & 12 & 7 & 4 & 37 & 96 & 71 & 36 & 25 & 15 & 61 & 0 & 3 \\ 0 & 5 & 6 & 1 & 0 & 5 & -1 & 3 & 0 & 1 & 2 & 1 & 6 & 5 & 4 & 3 & 3 & 5 & 4 & 3 \\ 2 & 3 & 4 & 3 & 0 & 1 & 3 & -1 & 4 & 1 & 0 & 15 & 36 & 25 & 12 & 7 & 5 & 23 & 0 & 1 \\ 1 & 12 & 17 & 6 & 1 & 12 & 0 & 4 & -1 & 0 & 1 & 0 & 1 & 0 & 1 & 0 & 2 & 2 & 7 & 4 \\ 2 & 9 & 12 & 5 & 0 & 7 & 1 & 1 & 0 & -1 & 0 & 5 & 12 & 7 & 4 & 1 & 3 & 9 & 4 & 3 \\ 1 & 4 & 7 & 4 & 1 & 4 & 2 & 0 & 1 & 0 & -1 & 4 & 7 & 4 & 1 & 0 & 0 & 4 & 1 & 0 \\ 0 & 31 & 48 & 17 & 6 & 37 & 1 & 15 & 0 & 5 & 4 & -1 & 0 & 1 & 2 & 3 & 3 & 1 & 20 & 9 \\ 1 & 80 & 127 & 48 & 17 & 96 & 6 & 36 & 1 & 12 & 7 & 0 & -1 & 0 & 1 & 4 & 4 & 0 & 49 & 20 \\ 2 & 61 & 96 & 37 & 12 & 71 & 5 & 25 & 0 & 7 & 4 & 1 & 0 & -1 & 0 & 1 & 3 & 1 & 36 & 15 \\ 1 & 30 & 49 & 20 & 7 & 36 & 4 & 12 & 1 & 4 & 1 & 2 & 1 & 0 & -1 & 0 & 0 & 0 & 17 & 6 \\ 2 & 23 & 36 & 15 & 4 & 25 & 3 & 7 & 0 & 1 & 0 & 3 & 4 & 1 & 0 & -1 & 1 & 3 & 12 & 5 \\ 0 & 11 & 20 & 9 & 4 & 15 & 3 & 5 & 2 & 3 & 0 & 3 & 4 & 3 & 0 & 1 & -1 & 1 & 6 & 1 \\ 0 & 49 & 80 & 31 & 12 & 61 & 5 & 23 & 2 & 9 & 4 & 1 & 0 & 1 & 0 & 3 & 1 & -1 & 30 & 11 \\ 1 & 0 & 1 & 2 & 1 & 0 & 4 & 0 & 7 & 4 & 1 & 20 & 49 & 36 & 17 & 12 & 6 & 30 & -1 & 0 \\ 0 & 1 & 4 & 3 & 2 & 3 & 3 & 1 & 4 & 3 & 0 & 9 & 20 & 15 & 6 & 5 & 1 & 11 & 0 & -1 \end{pmatrix}$$

8v12f_2

```
8v12f_2=Graph({ 0:[1, 2, 3, 4, 5, 6], 1:[0, 6, 7, 5, 2], 2:[0, 1, 5, 4, 3], 3:[0, 2, 4], 4:[0, 3, 2, 5], 5:[0, 4, 2, 1, 7, 6], 6:[0, 5, 7, 1], 7:[1, 6, 5]})
```



$$V = \begin{pmatrix} 0 & 0 & 0 & -1 \\ 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 4 & 1 & 0 \\ 4 & 16 & 8 & 1 \\ 4 & 13 & 7 & 2 \\ 4 & 12 & 7 & 0 \\ 4 & 9 & 6 & 1 \\ 4 & 7 & 5 & 2 \\ 4 & 6 & 5 & 0 \\ 4 & 4 & 4 & 1 \\ 4 & 3 & 3 & 2 \\ 4 & 2 & 3 & 0 \\ 4 & 1 & 2 & 1 \\ 4 & 1 & 1 & 2 \\ 8 & 1 & 3 & 0 \\ 12 & 1 & 3 & 2 \\ 16 & 1 & 4 & 1 \\ 4 & 0 & 0 & 1 \\ 8 & 0 & 1 & 0 \end{pmatrix}$$

$$G = \begin{pmatrix} -1 & 0 & 1 & 0 & 1 & 2 & 0 & 1 & 2 & 0 & 1 & 2 & 0 & 1 & 2 & 0 & 1 & 1 & 1 & 0 \\ 0 & -1 & 0 & 1 & 8 & 7 & 7 & 6 & 5 & 5 & 4 & 3 & 3 & 2 & 1 & 3 & 3 & 4 & 0 & 1 \\ 1 & 0 & -1 & 0 & 1 & 0 & 2 & 1 & 0 & 2 & 1 & 0 & 2 & 1 & 0 & 4 & 4 & 7 & 1 & 4 \\ 0 & 1 & 0 & -1 & 0 & 1 & 1 & 2 & 3 & 3 & 4 & 5 & 5 & 6 & 7 & 13 & 21 & 28 & 8 & 15 \\ 1 & 8 & 1 & 0 & -1 & 0 & 0 & 1 & 4 & 4 & 7 & 12 & 12 & 17 & 24 & 42 & 72 & 97 & 31 & 56 \\ 2 & 7 & 0 & 1 & 0 & -1 & 1 & 0 & 1 & 3 & 4 & 7 & 9 & 12 & 17 & 33 & 55 & 76 & 24 & 45 \\ 0 & 7 & 2 & 1 & 0 & 1 & -1 & 0 & 3 & 1 & 4 & 9 & 7 & 12 & 19 & 29 & 53 & 70 & 24 & 41 \\ 1 & 6 & 1 & 2 & 1 & 0 & 0 & -1 & 0 & 0 & 1 & 4 & 4 & 7 & 12 & 20 & 36 & 49 & 17 & 30 \\ 2 & 5 & 0 & 3 & 4 & 1 & 3 & 0 & -1 & 1 & 0 & 1 & 3 & 4 & 7 & 15 & 25 & 36 & 12 & 23 \\ 0 & 5 & 2 & 3 & 4 & 3 & 1 & 0 & 1 & -1 & 0 & 3 & 1 & 4 & 9 & 11 & 23 & 30 & 12 & 19 \\ 1 & 4 & 1 & 4 & 7 & 4 & 4 & 1 & 0 & 0 & -1 & 0 & 0 & 1 & 4 & 6 & 12 & 17 & 7 & 12 \\ 2 & 3 & 0 & 5 & 12 & 7 & 9 & 4 & 1 & 3 & 0 & -1 & 1 & 0 & 1 & 5 & 7 & 12 & 4 & 9 \\ 0 & 3 & 2 & 5 & 12 & 9 & 7 & 4 & 3 & 1 & 0 & 1 & -1 & 0 & 3 & 1 & 5 & 6 & 4 & 5 \\ 1 & 2 & 1 & 6 & 17 & 12 & 12 & 7 & 4 & 4 & 1 & 0 & 0 & -1 & 0 & 0 & 0 & 1 & 1 & 2 \\ 2 & 1 & 0 & 7 & 24 & 17 & 19 & 12 & 7 & 9 & 4 & 1 & 3 & 0 & -1 & 3 & 1 & 4 & 0 & 3 \\ 0 & 3 & 4 & 13 & 42 & 33 & 29 & 20 & 15 & 11 & 6 & 5 & 1 & 0 & 3 & -1 & 1 & 0 & 2 & 1 \\ 2 & 3 & 4 & 21 & 72 & 55 & 53 & 36 & 25 & 23 & 12 & 7 & 5 & 0 & 1 & 1 & -1 & 0 & 0 & 1 \\ 1 & 4 & 7 & 28 & 97 & 76 & 70 & 49 & 36 & 30 & 17 & 12 & 6 & 1 & 4 & 0 & 0 & -1 & 1 & 0 \\ 1 & 0 & 1 & 8 & 31 & 24 & 24 & 17 & 12 & 12 & 7 & 4 & 4 & 1 & 0 & 2 & 0 & 1 & -1 & 0 \\ 0 & 1 & 4 & 15 & 56 & 45 & 41 & 30 & 23 & 19 & 12 & 9 & 5 & 2 & 3 & 1 & 1 & 0 & 0 & -1 \end{pmatrix}$$

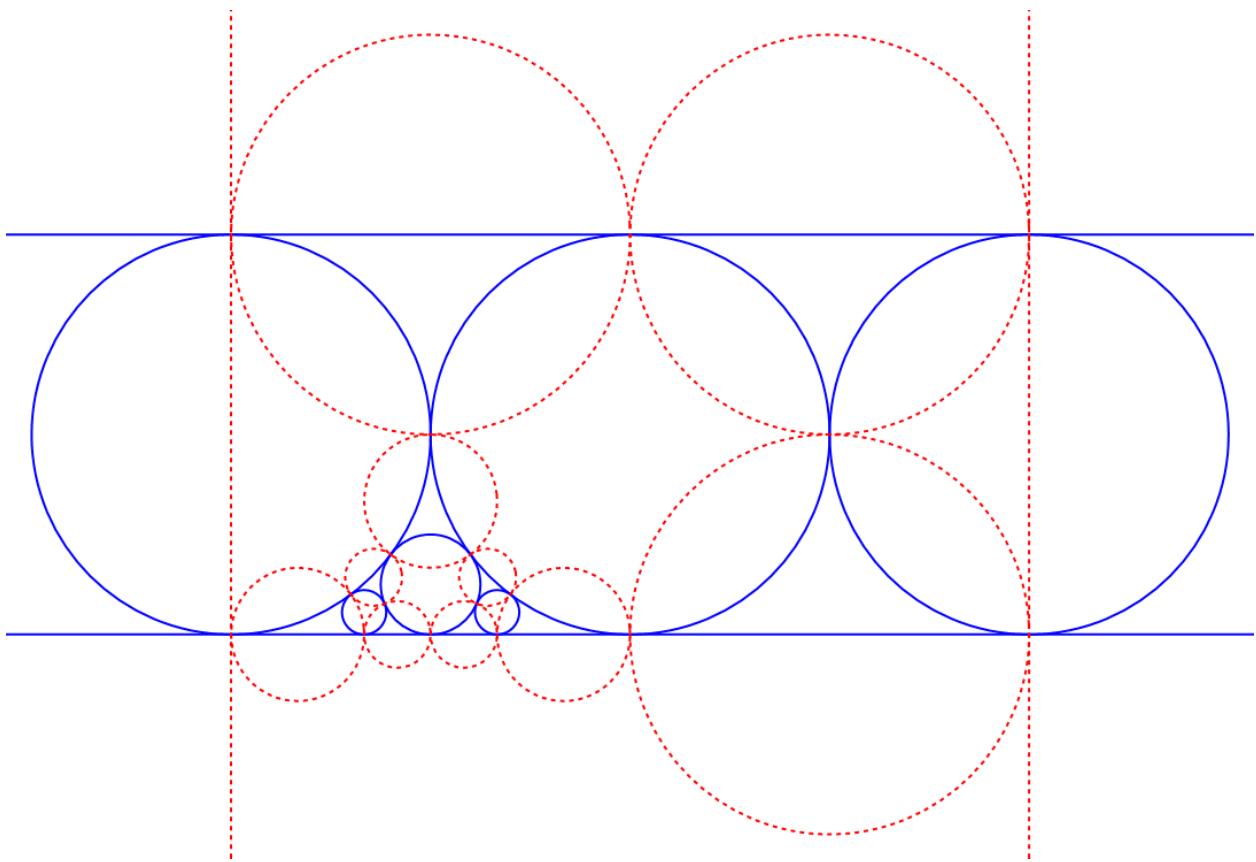
$$\left\{ \begin{pmatrix} 0 & 0 & 0 & 2 & -1 & 2 & 2 \\ 0 & 0 & 0 & 28 & -12 & 36 & 21 \\ 0 & 0 & 0 & 45 & -20 & 60 & 36 \\ 0 & 0 & 0 & 66 & -30 & 90 & 55 \\ 0 & 0 & 0 & 91 & -42 & 126 & 78 \\ 0 & 0 & 0 & 420 & -195 & 588 & 364 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 120 & -56 & 168 & 105 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 12 & -3 & 12 & 4 \\ 0 & 0 & 0 & 0 & 88 & -24 & 96 & 33 \\ 0 & 0 & 0 & 0 & 35 & -10 & 38 & 14 \\ 0 & 0 & 0 & 0 & 6 & -2 & 6 & 3 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 30 & -5 & 30 & 6 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 20 & -4 & 20 & 5 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 2 & -1 & 2 & 2 \\ 0 & 0 & 0 & 0 & 100 & -36 & 60 & 93 \\ 0 & 0 & 0 & 0 & 51 & -18 & 30 & 46 \\ 0 & 0 & 0 & 0 & 18 & -6 & 10 & 15 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 12 & -3 & 4 & 12 \\ 0 & 0 & 0 & 0 & 6 & -2 & 3 & 6 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 84 & -35 & 108 & 60 \\ 0 & 0 & 0 & 0 & 28 & -12 & 36 & 21 \\ 0 & 0 & 0 & 0 & 15 & -6 & 18 & 10 \\ 0 & 0 & 0 & 0 & 170 & -70 & 218 & 119 \\ 0 & 0 & 0 & 0 & 493 & -284 & 636 & 348 \\ 0 & 0 & 0 & 0 & 2870 & -1189 & 3710 & 2030 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 984 & -408 & 1272 & 697 \end{pmatrix}, \text{integral} \right\},$$

$$\left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 2 & -1 & 2 & 2 \\ 0 & 0 & 0 & 0 & 120 & -48 & 136 & 81 \\ 0 & 0 & 0 & 0 & 15 & -6 & 18 & 10 \\ 0 & 0 & 0 & 0 & 6 & -2 & 6 & 3 \\ 0 & 0 & 0 & 0 & 93 & -36 & 100 & 60 \\ 0 & 0 & 0 & 0 & 828 & -323 & 900 & 540 \\ 0 & 0 & 0 & 0 & 46 & -18 & 51 & 30 \\ 0 & 0 & 0 & 0 & 276 & -108 & 300 & 181 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 2 & -1 & 2 & 2 \\ 0 & 0 & 0 & 0 & 28 & -12 & 36 & 21 \\ 0 & 0 & 0 & 0 & 15 & -6 & 18 & 10 \\ 0 & 0 & 0 & 0 & 186 & -78 & 226 & 135 \\ 0 & 0 & 0 & 0 & 541 & -228 & 660 & 396 \\ 0 & 0 & 0 & 0 & 3420 & -1443 & 4180 & 2508 \\ 0 & 0 & 0 & 0 & 90 & -38 & 111 & 66 \\ 0 & 0 & 0 & 0 & 1080 & -456 & 1320 & 793 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 6 & 3 & 6 & -2 \\ 0 & 0 & 0 & 0 & 70 & 30 & 78 & -21 \\ 0 & 0 & 0 & 0 & 35 & 14 & 38 & -10 \\ 0 & 0 & 0 & 0 & 12 & 4 & 12 & -3 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 2 & 2 & 2 & -1 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 6 & 3 & -2 & 6 \\ 0 & 0 & 0 & 0 & 100 & 60 & -36 & 93 \\ 0 & 0 & 0 & 0 & 51 & 30 & -18 & 46 \\ 0 & 0 & 0 & 0 & 18 & 10 & -6 & 15 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 2 & 2 & -1 & 2 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}, \text{integral} \right\},$$

$$\left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 40 & -15 & 48 & 24 \\ 0 & 0 & 0 & 0 & 104 & -40 & 128 & 65 \\ 0 & 0 & 0 & 0 & 15 & -6 & 18 & 10 \\ 0 & 0 & 0 & 0 & 6 & -2 & 6 & 3 \\ 0 & 0 & 0 & 0 & 77 & -28 & 92 & 44 \\ 0 & 0 & 0 & 0 & 570 & -209 & 690 & 330 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 228 & -84 & 276 & 133 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 2 & -1 & 2 & 2 \\ 0 & 0 & 0 & 0 & 136 & -48 & 120 & 81 \\ 0 & 0 & 0 & 0 & 51 & -18 & 46 & 30 \\ 0 & 0 & 0 & 0 & 6 & -2 & 6 & 3 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 108 & -35 & 84 & 60 \\ 0 & 0 & 0 & 0 & 18 & -6 & 15 & 10 \\ 0 & 0 & 0 & 0 & 36 & -12 & 28 & 21 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & -2 & 3 & 6 & 6 \\ 0 & 0 & 0 & 0 & -28 & 44 & 92 & 77 \\ 0 & 0 & 0 & 0 & -15 & 24 & 48 & 40 \\ 0 & 0 & 0 & 0 & -6 & 10 & 18 & 15 \\ 0 & 0 & 0 & 0 & -1 & 2 & 2 & 2 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 2 & -1 & 2 & 2 \\ 0 & 0 & 0 & 0 & 36 & -20 & 60 & 45 \\ 0 & 0 & 0 & 0 & 21 & -12 & 36 & 28 \\ 0 & 0 & 0 & 0 & 10 & -6 & 18 & 15 \\ 0 & 0 & 0 & 0 & 3 & -2 & 6 & 6 \\ 0 & 0 & 0 & 0 & 4 & -3 & 12 & 12 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}, \text{integral} \right\}$$

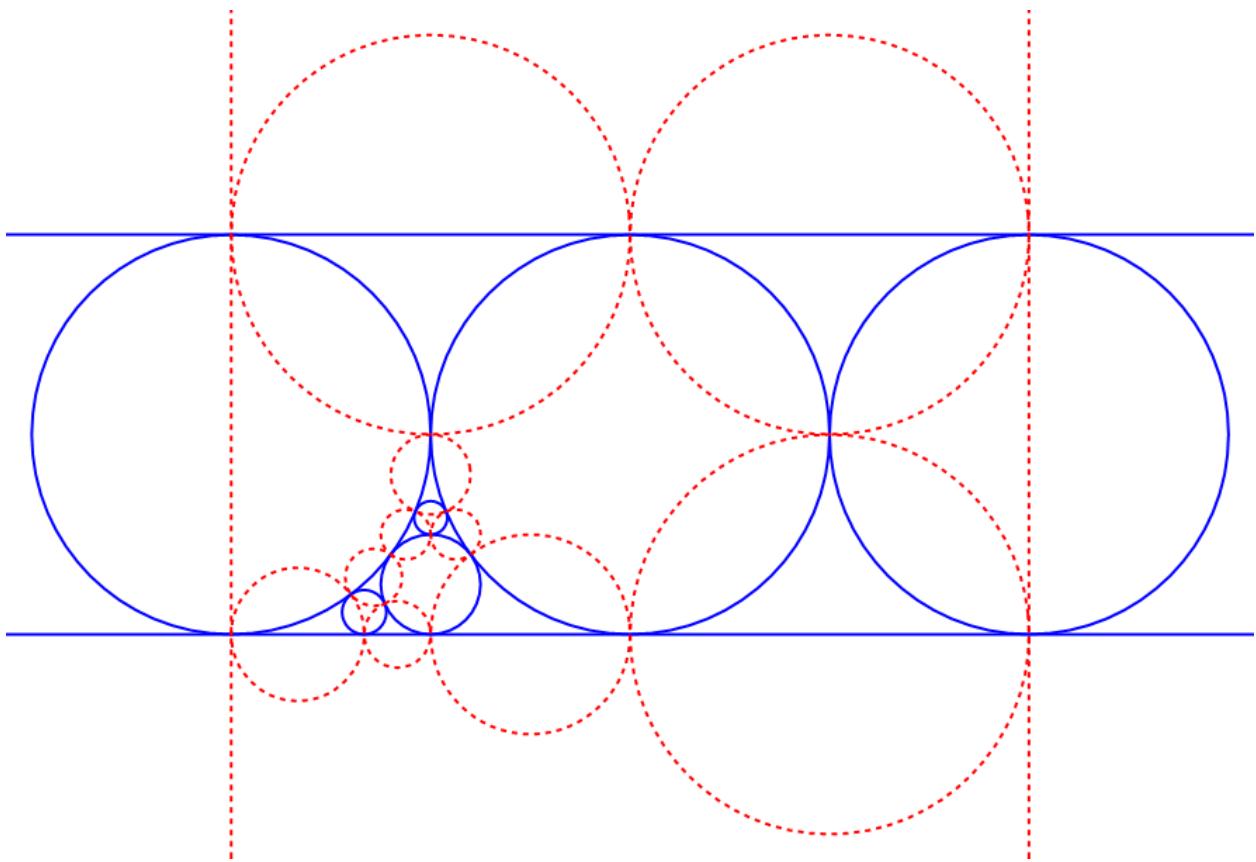
8v12f_3

8v12f_3=Graph({ 0:[1, 2, 3, 4, 5, 6, 7], 1:[0, 7, 6, 2], 2:[0, 1, 6, 4, 3], 3:[0, 2, 4], 4:[0, 3, 2, 6, 5], 5:[0, 4, 6], 6:[0, 5, 4, 2, 1, 7], 7:[0, 6, 1]})



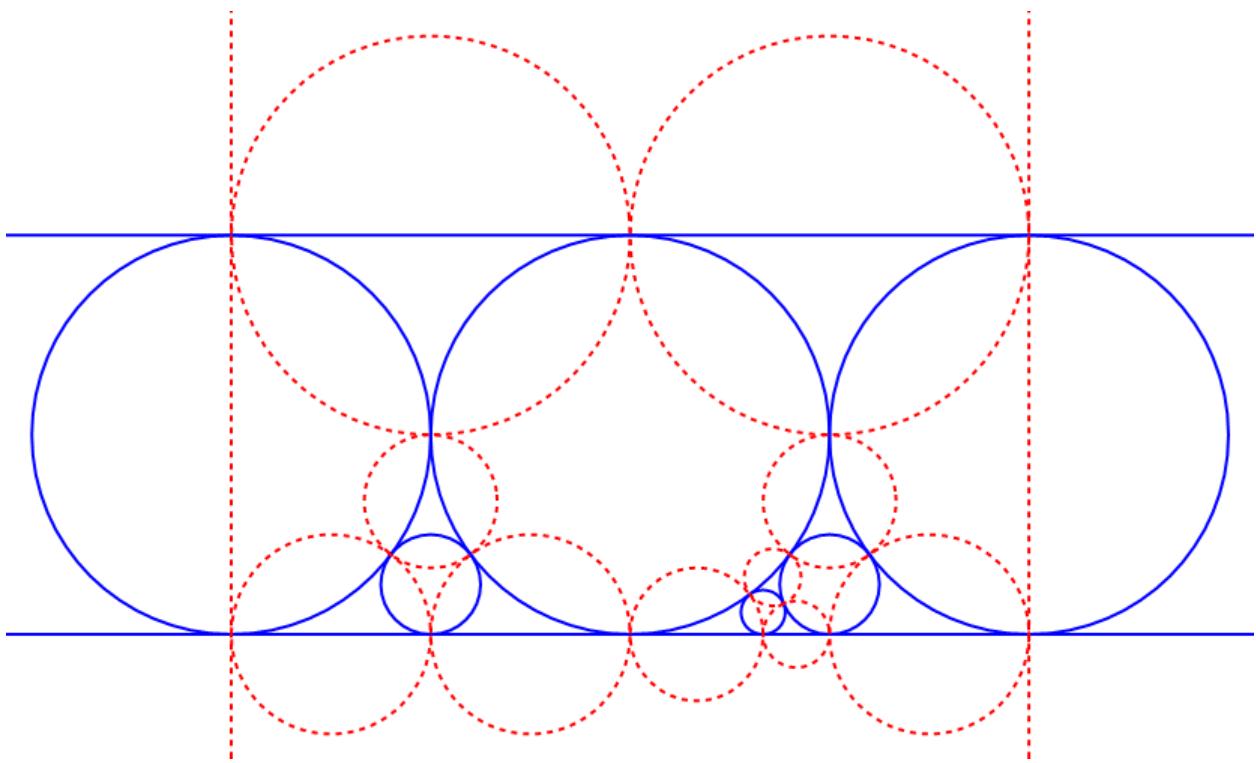
8v12f_4

```
8v12f_4=Graph({ 0:[1, 2, 3, 4, 5, 6], 1:[0, 6, 5, 2], 2:[0, 1, 5, 7, 4, 3], 3:[0, 2, 4], 4:[0, 3, 2, 7, 5],  
5:[0, 4, 7, 2, 1, 6], 6:[0, 5, 1], 7:[2, 5, 4]})
```



8v12f_5

```
8v12f_5=Graph({ 0:[1, 2, 3, 4, 5, 6, 7], 1:[0, 7, 4, 2], 2:[0, 1, 4, 3], 3:[0, 2, 4], 4:[0, 3, 2, 1, 7, 6, 5], 5:[0, 4, 6], 6:[0, 5, 4, 7], 7:[0, 6, 4, 1] })
```



$$V = \begin{pmatrix} 0 & 0 & 0 & -1 \\ 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 2 & 1 & 0 \\ 4 & 4 & 4 & 1 \\ 4 & 3 & 3 & 2 \\ 4 & 2 & 3 & 0 \\ 4 & 1 & 2 & 1 \\ 4 & 1 & 1 & 2 \\ 16 & 3 & 7 & 0 \\ 12 & 1 & 3 & 2 \\ 64 & 9 & 24 & 1 \\ 52 & 7 & 19 & 2 \\ 36 & 4 & 12 & 1 \\ 28 & 3 & 9 & 2 \\ 16 & 1 & 4 & 1 \\ 48 & 6 & 17 & 0 \\ 24 & 2 & 7 & 0 \\ 4 & 0 & 0 & 1 \\ 8 & 0 & 1 & 0 \end{pmatrix}$$

$$G = \begin{pmatrix} -1 & 0 & 1 & 0 & 1 & 2 & 0 & 1 & 2 & 0 & 2 & 1 & 2 & 1 & 2 & 1 & 0 & 0 & 1 & 0 \\ 0 & -1 & 0 & 1 & 4 & 3 & 3 & 2 & 1 & 7 & 3 & 24 & 19 & 12 & 9 & 4 & 17 & 7 & 0 & 1 \\ 1 & 0 & -1 & 0 & 1 & 0 & 2 & 1 & 0 & 8 & 4 & 31 & 24 & 17 & 12 & 7 & 24 & 12 & 1 & 4 \\ 0 & 1 & 0 & -1 & 0 & 1 & 1 & 2 & 3 & 9 & 9 & 40 & 33 & 24 & 19 & 12 & 31 & 17 & 4 & 7 \\ 1 & 4 & 1 & 0 & -1 & 0 & 0 & 1 & 4 & 10 & 12 & 49 & 40 & 31 & 24 & 17 & 40 & 24 & 7 & 12 \\ 2 & 3 & 0 & 1 & 0 & -1 & 1 & 0 & 1 & 9 & 7 & 40 & 31 & 24 & 17 & 12 & 33 & 19 & 4 & 9 \\ 0 & 3 & 2 & 1 & 0 & 1 & -1 & 0 & 3 & 1 & 5 & 10 & 9 & 8 & 7 & 6 & 9 & 7 & 4 & 5 \\ 1 & 2 & 1 & 2 & 1 & 0 & 0 & -1 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 2 & 2 & 1 & 2 \\ 2 & 1 & 0 & 3 & 4 & 1 & 3 & 0 & -1 & 7 & 1 & 24 & 17 & 12 & 7 & 4 & 19 & 9 & 0 & 3 \\ 0 & 7 & 8 & 9 & 10 & 9 & 1 & 0 & 7 & -1 & 5 & 0 & 1 & 2 & 3 & 4 & 1 & 3 & 6 & 5 \\ 2 & 3 & 4 & 9 & 12 & 7 & 5 & 0 & 1 & 5 & -1 & 12 & 7 & 4 & 1 & 0 & 9 & 3 & 0 & 1 \\ 1 & 24 & 31 & 40 & 49 & 40 & 10 & 1 & 24 & 0 & 12 & -1 & 0 & 1 & 4 & 7 & 0 & 4 & 17 & 12 \\ 2 & 19 & 24 & 33 & 40 & 31 & 9 & 0 & 17 & 1 & 7 & 0 & -1 & 0 & 1 & 4 & 1 & 3 & 12 & 9 \\ 1 & 12 & 17 & 24 & 31 & 24 & 8 & 1 & 12 & 2 & 4 & 1 & 0 & -1 & 0 & 1 & 0 & 0 & 7 & 4 \\ 2 & 9 & 12 & 19 & 24 & 17 & 7 & 0 & 7 & 3 & 1 & 4 & 1 & 0 & -1 & 0 & 3 & 1 & 4 & 3 \\ 1 & 4 & 7 & 12 & 17 & 12 & 6 & 1 & 4 & 4 & 0 & 7 & 4 & 1 & 0 & -1 & 4 & 0 & 1 & 0 \\ 0 & 17 & 24 & 31 & 40 & 33 & 9 & 2 & 19 & 1 & 9 & 0 & 1 & 0 & 3 & 4 & -1 & 1 & 12 & 7 \\ 0 & 7 & 12 & 17 & 24 & 19 & 7 & 2 & 9 & 3 & 3 & 4 & 3 & 0 & 1 & 0 & 1 & -1 & 4 & 1 \\ 1 & 0 & 1 & 4 & 7 & 4 & 4 & 1 & 0 & 6 & 0 & 17 & 12 & 7 & 4 & 1 & 12 & 4 & -1 & 0 \\ 0 & 1 & 4 & 7 & 12 & 9 & 5 & 2 & 3 & 5 & 1 & 12 & 9 & 4 & 3 & 0 & 7 & 1 & 0 & -1 \end{pmatrix}$$

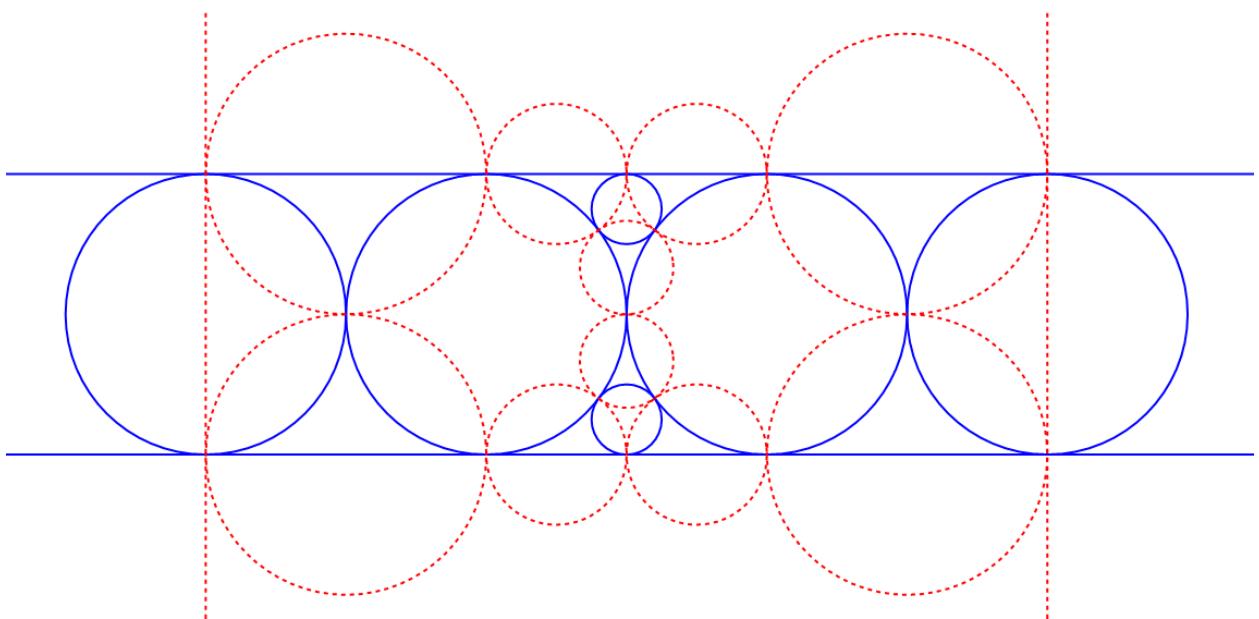
$$\left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 19 & -3 & -24 & 9 \\ 0 & 0 & 0 & 0 & 39 & -8 & -48 & 18 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 9 & -3 & -8 & 3 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 3 & 0 & -3 & 1 \\ 0 & 0 & 0 & 0 & 6 & 0 & -8 & 3 \end{pmatrix}, "integral"\right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 1 & -3 & 0 & 3 \\ 0 & 0 & 0 & 0 & 3 & -8 & 0 & 6 \\ 0 & 0 & 1 & 0 & 7 & -20 & 4 & 17 \\ 0 & 0 & 0 & 0 & 143 & -403 & 80 & 341 \\ 0 & 0 & 0 & 0 & 85 & -240 & 48 & 204 \\ 0 & 0 & 0 & 0 & 42 & -119 & 24 & 102 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 14 & -40 & 8 & 35 \end{pmatrix}, "integral"\right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 85 & -51 & 48 & 15 \\ 0 & 0 & 0 & 0 & 143 & -88 & 80 & 26 \\ 0 & 0 & 1 & 0 & 7 & -4 & 4 & 1 \\ 0 & 0 & 0 & 0 & 3 & -3 & 0 & 1 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 14 & -7 & 8 & 2 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 42 & -24 & 24 & 7 \end{pmatrix}, "integral"\right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 1 & -3 & 0 & 3 \\ 0 & 0 & 0 & 0 & 9 & -24 & -8 & 24 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 39 & -99 & -48 & 109 \\ 0 & 0 & 0 & 0 & 19 & -48 & -24 & 54 \\ 0 & 0 & 0 & 0 & 6 & -15 & -8 & 18 \\ 0 & 0 & 0 & 0 & 3 & -8 & -3 & 9 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}, "integral"\right\},$$

$$\left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 6 & -15 & 0 & 10 \\ 0 & 0 & 0 & 0 & 3 & -8 & 0 & 6 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 28 & -63 & 0 & 36 \\ 0 & 0 & 0 & 0 & 21 & -48 & 0 & 28 \\ 0 & 0 & 0 & 0 & 15 & -35 & 0 & 21 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 10 & -24 & 0 & 15 \end{pmatrix}, "integral"\right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 1 & -3 & 0 & 3 \\ 0 & 0 & 0 & 0 & 3 & -8 & 0 & 6 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 183 & -483 & -80 & 381 \\ 0 & 0 & 0 & 0 & 109 & -288 & -48 & 228 \\ 0 & 0 & 0 & 0 & 54 & -143 & -24 & 114 \\ 0 & 0 & 0 & 0 & 9 & -24 & -3 & 19 \\ 0 & 0 & 0 & 0 & 18 & -48 & -8 & 39 \end{pmatrix}, "integral"\right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 7 & 21 & 24 & -3 \\ 0 & 0 & 0 & 0 & 15 & 40 & 48 & -6 \\ 0 & 0 & 1 & 0 & 1 & 4 & 4 & -1 \\ 0 & 0 & 0 & 0 & 5 & 5 & 8 & -1 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 2 & 8 & 8 & -1 \end{pmatrix}, "integral"\right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 21 & -35 & 0 & 15 \\ 0 & 0 & 0 & 0 & 28 & -48 & 0 & 21 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 3 & -3 & 0 & 1 \\ 0 & 0 & 0 & 0 & 6 & -8 & 0 & 3 \\ 0 & 0 & 0 & 0 & 10 & -15 & 0 & 6 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 15 & -24 & 0 & 10 \end{pmatrix}, "integral"\right\},$$

$$\left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 3 & -3 & -8 & 9 \\ 0 & 0 & 0 & 0 & 9 & -8 & -24 & 24 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 9 & -3 & -24 & 19 \\ 0 & 0 & 0 & 0 & 3 & -8 & 6 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & -3 & 3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}, "integral"\right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 109 & -99 & -48 & 39 \\ 0 & 0 & 0 & 0 & 183 & -168 & -80 & 66 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 3 & -3 & 0 & 1 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 18 & -15 & -8 & 6 \\ 0 & 0 & 0 & 0 & 9 & -8 & -3 & 3 \\ 0 & 0 & 0 & 0 & 54 & -48 & -24 & 19 \end{pmatrix}, "integral"\right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & -1 & 5 & 8 & 5 \\ 0 & 0 & 0 & 0 & -3 & 16 & 24 & 12 \\ 0 & 0 & 1 & 0 & -1 & 4 & 4 & 1 \\ 0 & 0 & 0 & 0 & -3 & 21 & 24 & 7 \\ 0 & 0 & 0 & 0 & -1 & 8 & 8 & 2 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}, "integral"\right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 1 & -3 & 0 & 3 \\ 0 & 0 & 0 & 0 & 5 & -16 & 8 & 20 \\ 0 & 0 & 1 & 0 & 1 & -4 & 4 & 7 \\ 0 & 0 & 0 & 0 & 15 & -51 & 48 & 85 \\ 0 & 0 & 0 & 0 & 7 & -24 & 24 & 42 \\ 0 & 0 & 0 & 0 & 2 & -7 & 8 & 14 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}, "integral"\right\}$$

8v12f_7

8v12f_7=Graph({ 0:[1, 2, 3, 4, 5, 6], 1:[0, 6, 5, 7, 3, 2], 2:[0, 1, 3], 3:[0, 2, 1, 7, 5, 4], 4:[0, 3, 5], 5:[0, 4, 3, 7, 1, 6], 6:[0, 5, 1], 7:[1, 5, 3]})

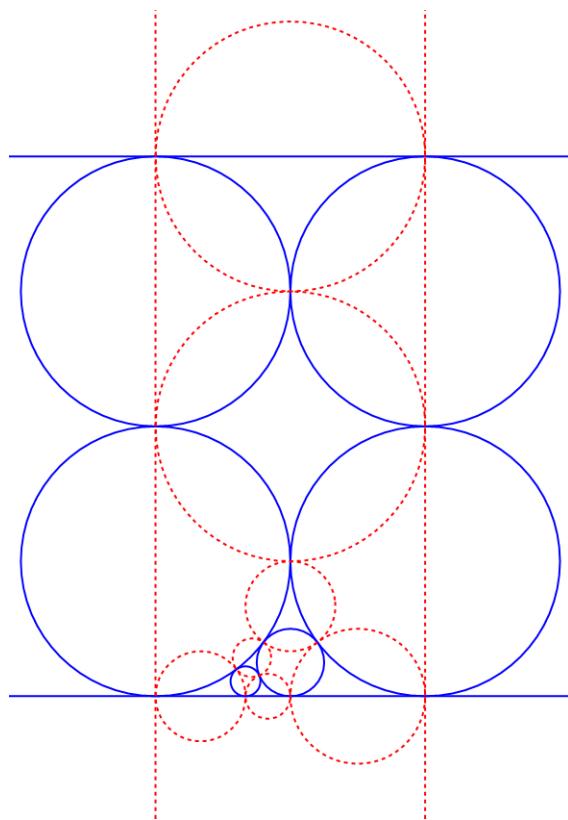


$$V = \begin{pmatrix} 0 & 0 & 0 & -1 \\ 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 1 & 1 & 0 \\ 4 & 1 & 2 & 1 \\ 4 & 1 & 1 & 2 \\ 12 & 2 & 5 & 0 \\ 20 & 2 & 5 & 4 \\ 36 & 4 & 12 & 1 \\ 28 & 3 & 9 & 2 \\ 16 & 1 & 4 & 1 \\ 32 & 3 & 9 & 4 \\ 48 & 4 & 12 & 7 \\ 24 & 2 & 7 & 0 \\ 32 & 2 & 7 & 4 \\ 24 & 1 & 5 & 0 \\ 28 & 1 & 5 & 2 \\ 36 & 1 & 6 & 1 \\ 4 & 0 & 0 & 1 \\ 12 & 0 & 1 & 0 \end{pmatrix}$$

-1	0	1	0	1	2	0	4	1	2	1	4	7	0	4	0	2	1	1	0
0	-1	0	1	2	1	5	5	12	9	4	9	12	7	7	5	5	6	0	1
1	0	-1	0	1	0	6	6	17	12	7	12	17	12	12	12	12	17	1	6
0	1	0	-1	0	1	1	5	6	5	4	7	12	5	9	7	9	12	2	5
1	2	1	0	-1	0	0	0	1	0	1	0	1	2	2	4	4	7	1	4
2	1	0	1	0	-1	5	1	12	7	4	5	6	9	5	9	7	12	0	5
0	5	6	1	0	5	-1	7	0	1	2	5	12	1	9	5	9	12	4	7
4	5	6	5	0	1	7	-1	12	5	2	1	0	9	1	9	5	12	0	7
1	12	17	6	1	12	0	12	-1	0	1	6	17	0	12	6	12	17	7	12
2	9	12	5	0	7	1	5	0	-1	0	1	6	1	5	5	7	12	4	9
1	4	7	4	1	4	2	2	1	0	-1	0	1	0	0	0	0	1	1	2
4	9	12	7	0	5	5	1	6	1	0	-1	0	5	1	7	5	12	2	9
7	12	17	12	1	6	12	0	17	6	1	0	-1	12	0	12	6	17	1	12
0	7	12	5	2	9	1	9	0	1	0	5	12	-1	7	1	5	6	4	5
4	7	12	9	2	5	9	1	12	5	0	1	0	7	-1	5	1	6	0	5
0	5	12	7	4	9	5	9	6	5	0	7	12	1	5	-1	1	0	2	1
2	5	12	9	4	7	9	5	12	7	0	5	6	5	1	1	-1	0	0	1
1	6	17	12	7	12	12	12	17	12	1	12	17	6	6	0	0	-1	1	0
1	0	1	2	1	0	4	0	7	4	1	2	1	4	0	2	0	1	-1	0
0	1	6	5	4	5	7	7	12	9	2	9	12	5	5	1	1	0	0	-1

8v9f 0 (8.2.14)

```
8v9f_0=Graph({0: [1, 2, 3, 4, 5], 1: [0, 6, 7], 2: [0, 7, 5, 4, 3], 3: [0, 2, 4], 4: [0, 3, 2, 5], 5: [0, 4, 2, 6], 6: [1, 5, 7], 7: [1, 6, 2]})
```

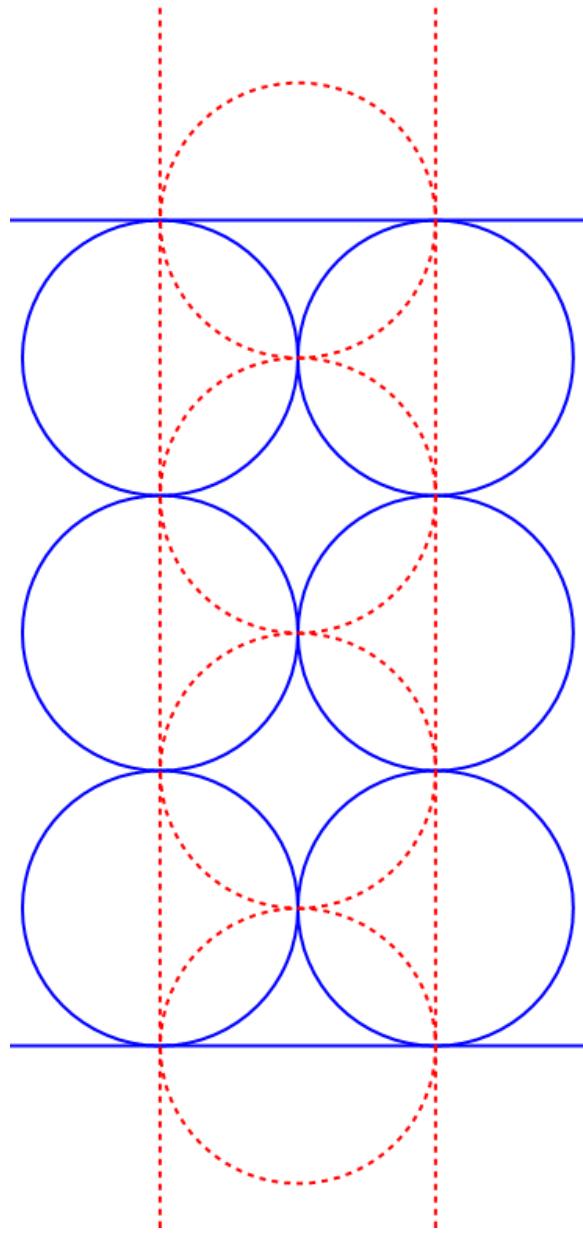


$$V = \begin{pmatrix} 0 & 0 & 0 & -1 \\ 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 3 & 1 & 0 \\ 4 & 9 & 6 & 1 \\ 4 & 7 & 5 & 2 \\ 4 & 6 & 5 & 0 \\ 4 & 4 & 4 & 1 \\ 4 & 3 & 3 & 2 \\ 4 & 2 & 3 & 0 \\ 4 & 1 & 2 & 1 \\ 4 & 1 & 1 & 2 \\ 12 & 1 & 2 & 3 \\ 8 & 1 & 0 & 3 \\ 16 & 1 & 1 & 4 \\ 8 & 0 & 0 & 1 \\ 4 & 0 & 1 & 0 \end{pmatrix}$$

$$\begin{aligned}
G = & \begin{pmatrix} -1 & 0 & 1 & 0 & 1 & 2 & 0 & 1 & 2 & 0 & 1 & 2 & 3 & 3 & 4 & 1 & 0 \\ 0 & -1 & 0 & 1 & 6 & 5 & 5 & 4 & 3 & 3 & 2 & 1 & 2 & 0 & 1 & 0 & 1 \\ 1 & 0 & -1 & 0 & 1 & 0 & 2 & 1 & 0 & 2 & 1 & 0 & 3 & 1 & 4 & 3 & 2 \\ 0 & 1 & 0 & -1 & 0 & 1 & 1 & 2 & 3 & 3 & 4 & 5 & 16 & 12 & 23 & 12 & 5 \\ 1 & 6 & 1 & 0 & -1 & 0 & 0 & 1 & 4 & 4 & 7 & 12 & 41 & 35 & 64 & 35 & 12 \\ 2 & 5 & 0 & 1 & 0 & -1 & 1 & 0 & 1 & 3 & 4 & 7 & 28 & 24 & 45 & 26 & 9 \\ 0 & 5 & 2 & 1 & 0 & 1 & -1 & 0 & 3 & 1 & 4 & 9 & 28 & 26 & 45 & 24 & 7 \\ 1 & 4 & 1 & 2 & 1 & 0 & 0 & -1 & 0 & 0 & 1 & 4 & 15 & 15 & 26 & 15 & 4 \\ 2 & 3 & 0 & 3 & 4 & 1 & 3 & 0 & -1 & 1 & 0 & 1 & 8 & 8 & 15 & 10 & 3 \\ 0 & 3 & 2 & 3 & 4 & 3 & 1 & 0 & 1 & -1 & 0 & 3 & 8 & 10 & 15 & 8 & 1 \\ 1 & 2 & 1 & 4 & 7 & 4 & 4 & 1 & 0 & 0 & -1 & 0 & 1 & 3 & 4 & 3 & 0 \\ 2 & 1 & 0 & 5 & 12 & 7 & 9 & 4 & 1 & 3 & 0 & -1 & 0 & 0 & 1 & 2 & 1 \\ 3 & 2 & 3 & 16 & 41 & 28 & 28 & 15 & 8 & 8 & 1 & 0 & -1 & 1 & 0 & 1 & 0 \\ 3 & 0 & 1 & 12 & 35 & 24 & 26 & 15 & 8 & 10 & 3 & 0 & 1 & -1 & 0 & 1 & 2 \\ 4 & 1 & 4 & 23 & 64 & 45 & 45 & 26 & 15 & 15 & 4 & 1 & 0 & 0 & -1 & 0 & 1 \\ 1 & 0 & 3 & 12 & 35 & 26 & 24 & 15 & 10 & 8 & 3 & 2 & 1 & 1 & 0 & -1 & 0 \\ 0 & 1 & 2 & 5 & 12 & 9 & 7 & 4 & 3 & 1 & 0 & 1 & 0 & 2 & 1 & 0 & -1 \end{pmatrix} \\
& \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 10 & 15 & 46 & -28 \\ 0 & 0 & 0 & 0 & 3 & 6 & 16 & -10 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 21 & 28 & 91 & -55 \\ 0 & 0 & 0 & 0 & 141 & 196 & 630 & -378 \\ 0 & 0 & 0 & 0 & 130 & 183 & 585 & -351 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 120 & 168 & 540 & -323 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 1 & 1 & -1 \\ 0 & 0 & 0 & 0 & 15 & 18 & 22 & -28 \\ 0 & 0 & 1 & 0 & 4 & 4 & 2 & -6 \\ 0 & 0 & 0 & 0 & 1 & 0 & 1 & -1 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 2 & 2 & -3 \\ 0 & 0 & 0 & 0 & 2 & 2 & 1 & -2 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 1 & 1 & -1 \\ 0 & 0 & 0 & 0 & 3 & 6 & 16 & -10 \\ 0 & 0 & 1 & 0 & 2 & 10 & 23 & -13 \\ 0 & 0 & 0 & 0 & 5 & 20 & 47 & -27 \\ 0 & 0 & 0 & 0 & 17 & 80 & 184 & -104 \\ 0 & 0 & 0 & 0 & 12 & 61 & 138 & -78 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 12 & 60 & 138 & -77 \end{pmatrix}, \text{integral} \right\}, \\
& \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 6 & 3 & 16 & -10 \\ 0 & 0 & 0 & 0 & 15 & 10 & 46 & -28 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 1 & -1 \\ 0 & 0 & 0 & 0 & 25 & 8 & 60 & -36 \\ 0 & 0 & 0 & 0 & 30 & 11 & 75 & -45 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 24 & 8 & 60 & -35 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 4 & 5 & -1 & 5 \\ 0 & 0 & 0 & 0 & 67 & 70 & -16 & 86 \\ 0 & 0 & 1 & 0 & 26 & 26 & -13 & 39 \\ 0 & 0 & 0 & 0 & 5 & 4 & -1 & 5 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 4 & 4 & -1 & 6 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 1 & 1 & -1 \\ 0 & 0 & 0 & 0 & 3 & 6 & 16 & -10 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 21 & 36 & 91 & -63 \\ 0 & 0 & 0 & 0 & 141 & 252 & 630 & -434 \\ 0 & 0 & 0 & 0 & 120 & 217 & 540 & -372 \\ 0 & 0 & 0 & 0 & 10 & 18 & 46 & -31 \\ 0 & 0 & 0 & 0 & 130 & 234 & 585 & -402 \end{pmatrix}, \text{integral} \right\}, \\
& \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 1 & 1 & -1 \\ 0 & 0 & 0 & 0 & 15 & 18 & 46 & -36 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 1 & -1 \\ 0 & 0 & 0 & 0 & 25 & 24 & 60 & -52 \\ 0 & 0 & 0 & 0 & 24 & 25 & 60 & -52 \\ 0 & 0 & 0 & 0 & 6 & 6 & 16 & -13 \\ 0 & 0 & 0 & 0 & 30 & 30 & 75 & -64 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 1 & 1 & -1 \\ 0 & 0 & 0 & 0 & -3 & 12 & 19 & -7 \\ 0 & 0 & 1 & 0 & -4 & 4 & 2 & 2 \\ 0 & 0 & 0 & 0 & -1 & 2 & 2 & 0 \\ 0 & 0 & 0 & 0 & -1 & 2 & 1 & 1 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 2 & -1 & 2 & 0 \\ 0 & 0 & 0 & 0 & 15 & -6 & 22 & -4 \\ 0 & 0 & 1 & 0 & 4 & -4 & 2 & 2 \\ 0 & 0 & 0 & 0 & 1 & 0 & 1 & -1 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 2 & -1 & 1 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}, \text{integral} \right\}
\end{aligned}$$

8v6f_0

8v6f_0=Graph({0: [1, 2, 3], 1: [0, 4, 5], 2: [0, 6, 3], 3: [0, 2, 7], 4: [1, 7, 5], 5: [1, 4, 6], 6: [2, 5, 7], 7: [3, 6, 4]})



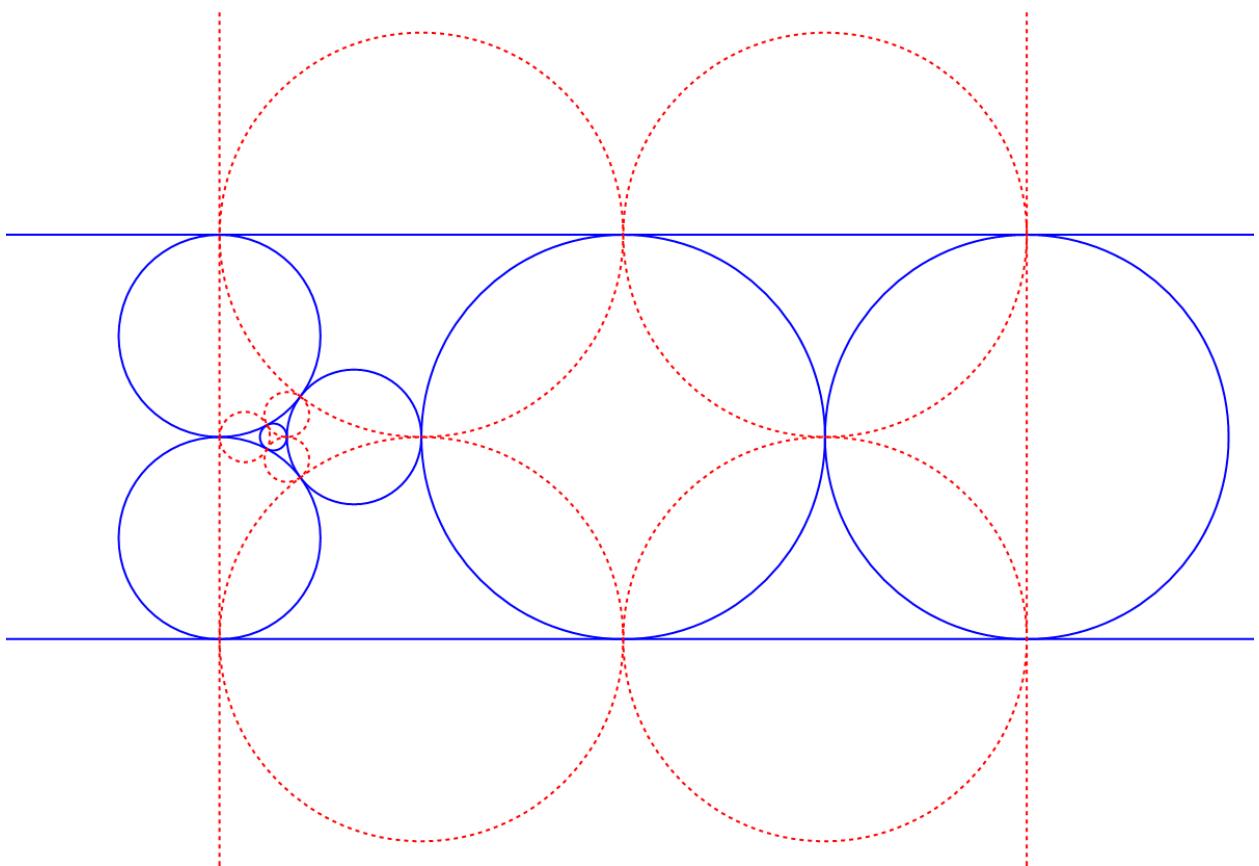
$$V = \begin{pmatrix} 0 & 0 & 0 & -1 \\ 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 1 & 1 & 0 \\ 4 & 1 & 2 & 1 \\ 4 & 1 & 1 & 2 \\ 12 & 1 & 2 & 3 \\ 8 & 1 & 0 & 3 \\ 16 & 1 & 1 & 4 \\ 28 & 1 & 2 & 5 \\ 24 & 1 & 0 & 5 \\ 36 & 1 & 1 & 6 \\ 12 & 0 & 0 & 1 \\ 4 & 0 & 1 & 0 \end{pmatrix}$$

$$G = \begin{pmatrix} -1 & 0 & 1 & 0 & 1 & 2 & 3 & 3 & 4 & 5 & 5 & 6 & 1 & 0 \\ 0 & -1 & 0 & 1 & 2 & 1 & 2 & 0 & 1 & 2 & 0 & 1 & 0 & 1 \\ 1 & 0 & -1 & 0 & 1 & 0 & 3 & 1 & 4 & 9 & 7 & 12 & 5 & 2 \\ 0 & 1 & 0 & -1 & 0 & 1 & 4 & 4 & 7 & 12 & 12 & 17 & 6 & 1 \\ 1 & 2 & 1 & 0 & -1 & 0 & 1 & 3 & 4 & 7 & 9 & 12 & 5 & 0 \\ 2 & 1 & 0 & 1 & 0 & -1 & 0 & 0 & 1 & 4 & 4 & 7 & 4 & 1 \\ 3 & 2 & 3 & 4 & 1 & 0 & -1 & 1 & 0 & 1 & 3 & 4 & 3 & 0 \\ 3 & 0 & 1 & 4 & 3 & 0 & 1 & -1 & 0 & 3 & 1 & 4 & 3 & 2 \\ 4 & 1 & 4 & 7 & 4 & 1 & 0 & 0 & -1 & 0 & 0 & 1 & 2 & 1 \\ 5 & 2 & 9 & 12 & 7 & 4 & 1 & 3 & 0 & -1 & 1 & 0 & 1 & 0 \\ 5 & 0 & 7 & 12 & 9 & 4 & 3 & 1 & 0 & 1 & -1 & 0 & 1 & 2 \\ 6 & 1 & 12 & 17 & 12 & 7 & 4 & 4 & 1 & 0 & 0 & -1 & 0 & 1 \\ 1 & 0 & 5 & 6 & 5 & 4 & 3 & 3 & 2 & 1 & 1 & 0 & -1 & 0 \\ 0 & 1 & 2 & 1 & 0 & 1 & 0 & 2 & 1 & 0 & 2 & 1 & 0 & -1 \end{pmatrix}$$

$$\left\{ \begin{pmatrix} 0 & 0 & 0 & 1 & 4 & 4 & -2 & 2 \\ 0 & 0 & 0 & 1 & 3 & 5 & -2 & 2 \\ 0 & 0 & 0 & 1 & -1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 4 & 4 & -3 & 4 \\ 0 & 0 & 0 & 0 & 2 & 2 & -2 & 3 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 1 & 0 & 0 & 2 & -2 \\ 0 & 0 & 0 & 1 & -1 & 1 & 2 & -2 \\ 0 & 0 & 0 & 1 & 3 & 5 & 4 & -4 \\ 0 & 0 & 0 & 1 & 4 & 4 & 4 & -4 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 2 & 2 & 3 & -2 \\ 0 & 0 & 0 & 0 & 4 & 4 & 4 & -3 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 1 & 0 & 0 & 2 & -2 \\ 0 & 0 & 0 & 1 & -1 & 1 & 2 & -2 \\ 0 & 0 & 0 & 1 & 11 & 13 & 52 & -20 \\ 0 & 0 & 0 & 1 & 12 & 12 & 52 & -20 \\ 0 & 0 & 0 & 1 & 4 & 4 & 18 & -8 \\ 0 & 0 & 0 & 1 & 3 & 5 & 18 & -8 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 6 & 6 & 26 & -9 \end{pmatrix}, \text{integral} \right\}$$

$$\left\{ \begin{pmatrix} 0 & 0 & 0 & 1 & 12 & 12 & -18 & 50 \\ 0 & 0 & 0 & 1 & 11 & 13 & -18 & 50 \\ 0 & 0 & 0 & 1 & -1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 4 & 4 & -6 & 16 \\ 0 & 0 & 0 & 1 & 3 & 5 & -6 & 16 \\ 0 & 0 & 0 & 0 & 6 & 6 & -9 & 26 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & -1 & 2 & 2 & 0 \\ 0 & 0 & 0 & 1 & -1 & 1 & 2 & -2 \\ 0 & 0 & 0 & 1 & -1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 2 & 0 & 2 \\ 0 & 0 & 0 & 2 & -3 & 2 & 2 & -2 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 1 & 0 & 0 & 2 & -2 \\ 0 & 0 & 0 & 0 & 2 & -1 & 2 & 0 \\ 0 & 0 & 0 & 0 & 2 & -1 & 0 & 2 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 2 & 0 & -1 & 2 & -2 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \end{pmatrix}, \text{integral} \right\}$$

8v9f_1



$$V = \begin{pmatrix} 0 & 0 & 0 & -1 \\ 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & \frac{1}{2} & 1 & 0 \\ 8 & \frac{3}{2} & 2 & 3 \\ 16 & \frac{9}{2} & 3 & 8 \\ 8 & \frac{1}{2} & 2 & 1 \\ 8 & \frac{1}{2} & 1 & 2 \\ 8 & 1 & 0 & 3 \\ 24 & \frac{9}{2} & 3 & 10 \\ 32 & \frac{15}{2} & 4 & 15 \\ 16 & 4 & 1 & 8 \\ 16 & \frac{1}{2} & 3 & 0 \\ 24 & \frac{1}{2} & 3 & 2 \\ 32 & \frac{1}{2} & 4 & 1 \\ 8 & 0 & 0 & 1 \\ 16 & 0 & 1 & 0 \end{pmatrix}$$

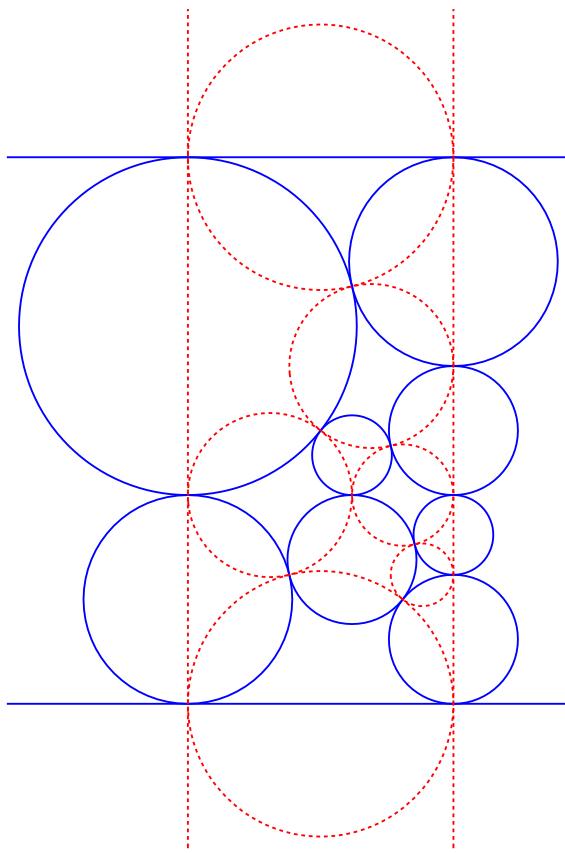
$$G = \begin{pmatrix} -1 & 0 & 1 & 0 & 3 & 8 & 1 & 2 & 3 & 10 & 15 & 8 & 0 & 2 & 1 & 1 & 0 \\ 0 & -1 & 0 & 1 & 2 & 3 & 2 & 1 & 0 & 3 & 4 & 1 & 3 & 3 & 4 & 0 & 1 \\ 1 & 0 & -1 & 0 & 1 & 0 & 3 & 2 & 1 & 2 & 1 & 0 & 8 & 10 & 15 & 3 & 8 \\ 0 & 1 & 0 & -1 & 0 & 1 & 0 & 1 & 2 & 3 & 4 & 3 & 1 & 3 & 4 & 2 & 3 \\ 3 & 2 & 1 & 0 & -1 & 0 & 1 & 0 & 1 & 0 & 1 & 2 & 8 & 8 & 15 & 3 & 10 \\ 8 & 3 & 0 & 1 & 0 & -1 & 8 & 3 & 2 & 1 & 0 & 1 & 31 & 33 & 56 & 10 & 33 \\ 1 & 2 & 3 & 0 & 1 & 8 & -1 & 0 & 3 & 8 & 15 & 10 & 0 & 0 & 1 & 1 & 2 \\ 2 & 1 & 2 & 1 & 0 & 3 & 0 & -1 & 0 & 1 & 4 & 3 & 3 & 1 & 4 & 0 & 3 \\ 3 & 0 & 1 & 2 & 1 & 2 & 3 & 0 & -1 & 0 & 1 & 0 & 10 & 8 & 15 & 1 & 8 \\ 10 & 3 & 2 & 3 & 0 & 1 & 8 & 1 & 0 & -1 & 0 & 1 & 33 & 31 & 56 & 8 & 33 \\ 15 & 4 & 1 & 4 & 1 & 0 & 15 & 4 & 1 & 0 & -1 & 0 & 56 & 56 & 97 & 15 & 56 \\ 8 & 1 & 0 & 3 & 2 & 1 & 10 & 3 & 0 & 1 & 0 & -1 & 33 & 33 & 56 & 8 & 31 \\ 0 & 3 & 8 & 1 & 8 & 31 & 0 & 3 & 10 & 33 & 56 & 33 & -1 & 1 & 0 & 2 & 1 \\ 2 & 3 & 10 & 3 & 8 & 33 & 0 & 1 & 8 & 31 & 56 & 33 & 1 & -1 & 0 & 0 & 1 \\ 1 & 4 & 15 & 4 & 15 & 56 & 1 & 4 & 15 & 56 & 97 & 56 & 0 & 0 & -1 & 1 & 0 \\ 1 & 0 & 3 & 2 & 3 & 10 & 1 & 0 & 1 & 8 & 15 & 8 & 2 & 0 & 1 & -1 & 0 \\ 0 & 1 & 8 & 3 & 10 & 33 & 2 & 3 & 8 & 33 & 56 & 31 & 1 & 1 & 0 & 0 & -1 \end{pmatrix}$$

$$\left\{ \begin{pmatrix} 0 & 0 & 0 & 1 & 0 & 0 & 1 & -1 \\ 0 & 0 & 0 & 8 & -2 & 5 & 4 & -4 \\ 0 & 0 & 0 & 0 & -1 & 8 & 8 & 0 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 2 & -1 & 2 \\ 0 & 0 & 0 & 8 & -2 & 5 & 4 & -4 \\ 0 & 0 & 0 & 0 & -1 & 8 & 0 & 8 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 7 & -1 & 8 & 0 & 1 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 1 & 0 & 0 & 1 & -1 \\ 0 & 0 & 0 & 1 & 14 & -17 & 2 & 1 \\ 0 & 0 & 0 & 6 & 79 & -100 & 12 & 6 \end{pmatrix}, \text{integral} \right\},$$

$$\left\{ \begin{pmatrix} 0 & 0 & 0 & 0 & -6 & 36 & 37 & 20 \\ 0 & 0 & 0 & 8 & -2 & 5 & 4 & -4 \\ 0 & 0 & 0 & 2 & -1 & 4 & 4 & 2 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 1 & 0 & 0 & 1 & -1 \\ 0 & 0 & 0 & 8 & 6 & 13 & 12 & -12 \\ 0 & 0 & 0 & 2 & 55 & 60 & 60 & -54 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 1 & 2 & 2 & 2 & -2 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 1 & 2 & 2 & -1 & 1 \\ 0 & 0 & 0 & 8 & 6 & 13 & -4 & 4 \\ 0 & 0 & 0 & 2 & 55 & 60 & -52 & 58 \end{pmatrix}, \text{integral} \right\},$$

$$\left\{ \begin{pmatrix} 0 & 0 & 0 & 2 & -8 & 46 & 27 & 44 \\ 0 & 0 & 0 & 8 & -2 & 5 & 4 & -4 \\ 0 & 0 & 0 & 2 & -1 & 4 & 4 & 2 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 1 & 0 & 0 & 1 & -1 \\ 0 & 0 & 0 & 2 & 0 & -1 & 2 & 0 \\ 0 & 0 & 0 & 8 & -1 & 0 & 8 & 0 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 6 & 1 & -4 & 4 & -2 \end{pmatrix}, \text{integral} \right\}, \left\{ \begin{pmatrix} 0 & 0 & 0 & 7 & -4 & 16 & 33 & 25 \\ 0 & 0 & 0 & 5 & -2 & 7 & 10 & 5 \\ 0 & 0 & 0 & 2 & -1 & 4 & 4 & 2 \end{pmatrix}, \text{integral} \right\},$$

Square Cupola



$$V = \begin{pmatrix} 0 & 0 & 0 & -1 \\ 0 & 0 & -1 & 0 \\ 0 & \frac{1}{2}(1 + \sqrt{5}) & 0 & 1 \\ 0 & \textcircled{0.786...} & 1 & 0 \\ 4 & \frac{1}{2}(1 + \sqrt{5}) & \sqrt{2(-1 + \sqrt{5})} & \sqrt{5} \\ 2\sqrt{2(1 + \sqrt{5})} & \sqrt{\frac{1}{2}(11 + 5\sqrt{5})} & 1 & 2\sqrt{2 + \sqrt{5}} \\ 2(1 + \sqrt{5}) & \frac{1}{2}(3 + \sqrt{5}) & 0 & 2 + \sqrt{5} \\ 4\sqrt{2 + \sqrt{5}} & \sqrt{2 + \sqrt{5}} & 1 & 2\sqrt{2 + \sqrt{5}} \\ 2(1 + \sqrt{5}) & 1 & \sqrt{2(1 + \sqrt{5})} & 1 \\ 4\sqrt{2 + \sqrt{5}} & \sqrt{\frac{1}{2}(1 + \sqrt{5})} & \sqrt{5} & \sqrt{2(1 + \sqrt{5})} \\ 4(2 + \sqrt{5}) & \frac{1}{2}(3 + \sqrt{5}) & \sqrt{2(1 + \sqrt{5})} & 4 + \sqrt{5} \\ 2(3 + \sqrt{5}) & \frac{1}{2}(1 + \sqrt{5}) & 0 & 2 + \sqrt{5} \\ 2\sqrt{22 + 10\sqrt{5}} & \sqrt{\frac{1}{2}(1 + \sqrt{5})} & 1 & 2\sqrt{2 + \sqrt{5}} \\ 2(3 + \sqrt{5}) & \frac{1}{2}(-1 + \sqrt{5}) & \sqrt{2(-1 + \sqrt{5})} & \sqrt{5} \\ 4(2 + \sqrt{5}) & 1 & 0 & 2 + \sqrt{5} \\ 2\sqrt{58 + 26\sqrt{5}} & \textcircled{0.786...} & 1 & 2\sqrt{2 + \sqrt{5}} \\ 2(3 + \sqrt{5}) & 0 & 0 & 1 \\ 2\sqrt{2(1 + \sqrt{5})} & 0 & 1 & 0 \end{pmatrix}$$

-1	0	1	0	$\sqrt{5}$	$2\sqrt{2+\sqrt{5}}$	$2+\sqrt{5}$	$2\sqrt{2+\sqrt{5}}$	1	$\sqrt{2(1+\sqrt{5})}$	$4+\sqrt{5}$	$2+\sqrt{5}$	$2\sqrt{2+\sqrt{5}}$	$\sqrt{5}$	$2+\sqrt{5}$	$2\sqrt{2+\sqrt{5}}$	1	0	
0	-1	0	1	$\sqrt{2(-1+\sqrt{5})}$	1	0	1	$\sqrt{2(1+\sqrt{5})}$	$\sqrt{5}$	$\sqrt{2(1+\sqrt{5})}$	0	1	$\sqrt{2(1+\sqrt{5})}$	0	1	0	1	
1	0	-1	0	1	0	1	$\sqrt{2(1-\sqrt{5})}$	$2+\sqrt{5}$	$2\sqrt{2+\sqrt{5}}$	$3+2\sqrt{5}$	$2+\sqrt{5}$	$\sqrt{22+10\sqrt{5}}$	$4+\sqrt{5}$	$5+2\sqrt{5}$	$2\sqrt{22+10\sqrt{5}}$	$3+2\sqrt{5}$	$2\sqrt{2+\sqrt{5}}$	
0	1	0	-1	0	1	$\sqrt{2(1+\sqrt{5})}$	$\sqrt{5}$	0	1	$2\sqrt{2+\sqrt{5}}$	$2\sqrt{2+\sqrt{5}}$	$2+\sqrt{5}$	$\sqrt{2(1+\sqrt{5})}$	$\sqrt{22+10\sqrt{5}}$	$3+2\sqrt{5}$	$2\sqrt{2+\sqrt{5}}$	1	
$\sqrt{5}$	$\sqrt{2(-1+\sqrt{5})}$	1	0	-1	0	1	0	1	0	1	$\sqrt{5}$	$\sqrt{2(1+\sqrt{5})}$	$\sqrt{5}$	$4+\sqrt{5}$	$4\sqrt{2+\sqrt{5}}$	$4+\sqrt{5}$	$\sqrt{2(1+\sqrt{5})}$	
$2\sqrt{2+\sqrt{5}}$	1	0	1	0	-1	0	1	$\sqrt{22+10\sqrt{5}}$	$2+\sqrt{5}$	$\sqrt{22+10\sqrt{5}}$	$2\sqrt{2+\sqrt{5}}$	$3+2\sqrt{5}$	$4+\sqrt{5}$	$2\sqrt{22+10\sqrt{5}}$	$11+4\sqrt{5}$	$2\sqrt{22+10\sqrt{5}}$	$3+2\sqrt{5}$	
$2+\sqrt{5}$	0	0	1	$\sqrt{2(1+\sqrt{5})}$	1	0	-1	0	$3+2\sqrt{5}$	$2\sqrt{2+\sqrt{5}}$	$2+\sqrt{5}$	1	$2\sqrt{2+\sqrt{5}}$	$4+\sqrt{5}$	$3+2\sqrt{5}$	$2\sqrt{22+10\sqrt{5}}$	$5+2\sqrt{5}$	
$2\sqrt{2-\sqrt{5}}$	1	$\sqrt{2(1+\sqrt{5})}$	$\sqrt{5}$	0	1	0	-1	$2\sqrt{2+\sqrt{5}}$	1	0	0	1	$\sqrt{2(1+\sqrt{5})}$	$2\sqrt{2+\sqrt{5}}$	$3+2\sqrt{5}$	$\sqrt{22+10\sqrt{5}}$	$2+\sqrt{5}$	
1	$\sqrt{2(1+\sqrt{5})}$	$2+\sqrt{5}$	0	1	$\sqrt{22+10\sqrt{5}}$	$3+2\sqrt{5}$	$2\sqrt{2+\sqrt{5}}$	-1	0	$2+\sqrt{5}$	$4+\sqrt{5}$	$2\sqrt{2+\sqrt{5}}$	1	$3+2\sqrt{5}$	$\sqrt{22+10\sqrt{5}}$	$2+\sqrt{5}$	0	
$\sqrt{2(1-\sqrt{5})}$	$\sqrt{5}$	$2\sqrt{2-\sqrt{5}}$	1	0	$2+\sqrt{5}$	$2\sqrt{2-\sqrt{5}}$	1	0	0	-1	0	$\sqrt{2(1+\sqrt{5})}$	1	0	$2\sqrt{2-\sqrt{5}}$	$2+\sqrt{5}$	$2\sqrt{2-\sqrt{5}}$	
$4+\sqrt{5}$	$\sqrt{2(1-\sqrt{5})}$	$3+2\sqrt{5}$	$2\sqrt{2-\sqrt{5}}$	1	$\sqrt{22+10\sqrt{5}}$	$2+\sqrt{5}$	0	$2+\sqrt{5}$	0	-1	1	0	1	$2+\sqrt{5}$	$\sqrt{22+10\sqrt{5}}$	$3+2\sqrt{5}$	$2\sqrt{2-\sqrt{5}}$	
$2+\sqrt{5}$	0	0	$2+\sqrt{5}$	$2\sqrt{2-\sqrt{5}}$	$\sqrt{5}$	$2\sqrt{2-\sqrt{5}}$	1	0	0	$4+\sqrt{5}$	$\sqrt{2(1+\sqrt{5})}$	1	-1	$\sqrt{5}$	1	$2\sqrt{2-\sqrt{5}}$	$5+2\sqrt{5}$	$2\sqrt{2-\sqrt{5}}$
$2\sqrt{2+\sqrt{5}}$	1	$\sqrt{22+10\sqrt{5}}$	$2+\sqrt{5}$	$\sqrt{2(1+\sqrt{5})}$	$3+2\sqrt{5}$	$2\sqrt{2+\sqrt{5}}$	1	$2\sqrt{2+\sqrt{5}}$	1	0	0	-1	0	0	1	$\sqrt{2(1+\sqrt{5})}$	$\sqrt{5}$	
$\sqrt{5}$	$\sqrt{2(-1+\sqrt{5})}$	$4+\sqrt{5}$	$\sqrt{2(1-\sqrt{5})}$	$\sqrt{5}$	$4\sqrt{2-\sqrt{5}}$	$4+\sqrt{5}$	$\sqrt{2(1-\sqrt{5})}$	1	0	1	$\sqrt{5}$	0	-1	1	0	1	0	
$2+\sqrt{5}$	0	$5+2\sqrt{5}$	$\sqrt{22+10\sqrt{5}}$	$4+\sqrt{5}$	$2\sqrt{2+\sqrt{5}}$	$3+2\sqrt{5}$	$2\sqrt{2+\sqrt{5}}$	$3+2\sqrt{5}$	$2\sqrt{2+\sqrt{5}}$	$2+\sqrt{5}$	1	0	1	-1	0	1	$\sqrt{2(1-\sqrt{5})}$	
$2\sqrt{2-\sqrt{5}}$	1	$2\sqrt{22+10\sqrt{5}}$	$3+2\sqrt{5}$	$4\sqrt{2-\sqrt{5}}$	$11+4\sqrt{5}$	$2\sqrt{22+10\sqrt{5}}$	$3+2\sqrt{5}$	$\sqrt{22+10\sqrt{5}}$	$2+\sqrt{5}$	$\sqrt{22+10\sqrt{5}}$	$2\sqrt{2+\sqrt{5}}$	1	0	0	-1	0	1	
1	0	$3+2\sqrt{5}$	$2\sqrt{2+\sqrt{5}}$	$4+\sqrt{5}$	$2\sqrt{22+10\sqrt{5}}$	$5+2\sqrt{5}$	$\sqrt{22+10\sqrt{5}}$	$3+2\sqrt{5}$	$2\sqrt{2+\sqrt{5}}$	$2+\sqrt{5}$	$\sqrt{2(1+\sqrt{5})}$	1	1	0	-1	0	0	
0	1	$2\sqrt{2+\sqrt{5}}$	1	$\sqrt{2(1+\sqrt{5})}$	$3+2\sqrt{5}$	$\sqrt{22+10\sqrt{5}}$	$2+\sqrt{5}$	0	1	$2\sqrt{2+\sqrt{5}}$	$2\sqrt{2+\sqrt{5}}$	$\sqrt{5}$	0	$\sqrt{2(1+\sqrt{5})}$	1	0	-1	

$$\left\{ \begin{array}{ccccccccc} 0 & 0 & 1 & -1 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 3 & -4 & -2 & 5 & 4 & -3 & 5 & 7 \\ 0 & 0 & 11 & -16 & -2 & 10 & 10 & -6 & 12 & 26 \\ 0 & 0 & 10 & -15 & -2 & 10 & 10 & -6 & 12 & 26 \\ 0 & 0 & 5 & -8 & 0 & 5 & 5 & -3 & 6 & 13 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 5 & -8 & -1 & 5 & 6 & -3 & 6 & 13 \\ 0 & 0 & 6 & -8 & -2 & 10 & 6 & -5 & 8 & 14 \\ 0 & 0 & 3 & -4 & -1 & 5 & 3 & -3 & 5 & 7 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{array} \right\}, \text{integral} \Big\}, \left\{ \begin{array}{ccccccccc} 0 & 0 & 4 & -1 & -1 & 1 & 3 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & 0 & 1 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & -2 & -2 & 4 & 2 & 2 & 0 \\ 0 & 0 & 3 & 0 & 0 & 1 & 3 & 1 & 0 & -1 \\ 0 & 0 & 0 & 0 & -2 & -1 & 4 & 2 & 2 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 3 & 0 & -1 & 1 & 3 & 1 & 1 & -1 \\ 0 & 0 & 3 & 0 & -3 & -1 & 7 & 3 & 2 & 0 \end{array} \right\}, \text{integral} \Big\}, \left\{ \begin{array}{ccccccccc} 0 & 0 & 11 & 15 & -2 & -6 & 10 & 10 & 12 & -5 \\ 0 & 0 & 3 & 4 & -2 & -3 & 4 & 5 & 5 & -1 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 5 & 8 & 0 & -3 & 5 & 5 & 6 & -3 \\ 0 & 0 & 6 & 8 & -2 & -5 & 6 & 10 & 8 & -2 \\ 0 & 0 & 5 & 8 & -1 & -3 & 6 & 5 & 6 & -3 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 3 & 4 & -1 & -3 & 3 & 5 & 5 & -1 \\ 0 & 0 & 10 & 16 & -2 & -6 & 10 & 10 & 12 & -5 \end{array} \right\}, \text{integral} \Big\}$$

$$\left\{ \begin{array}{c} \text{integral} \\ \text{integral} \end{array} \right\}, \left\{ \begin{array}{c} \text{integral} \\ \text{integral} \end{array} \right\}$$